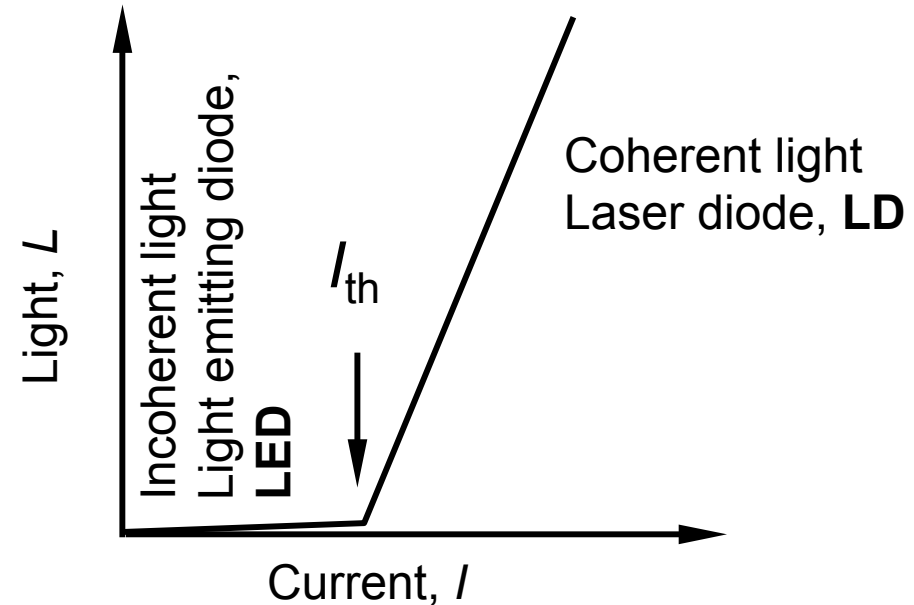
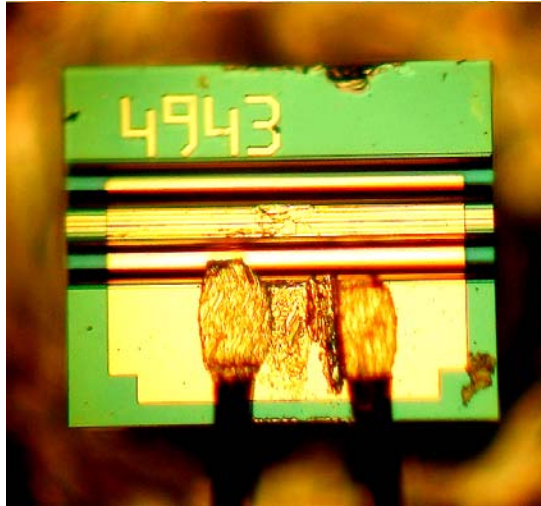

Quantum fluctuations in small lasers

A.F.J. Levi

EPFL Colloquium, July 29, 2009

The laser diode



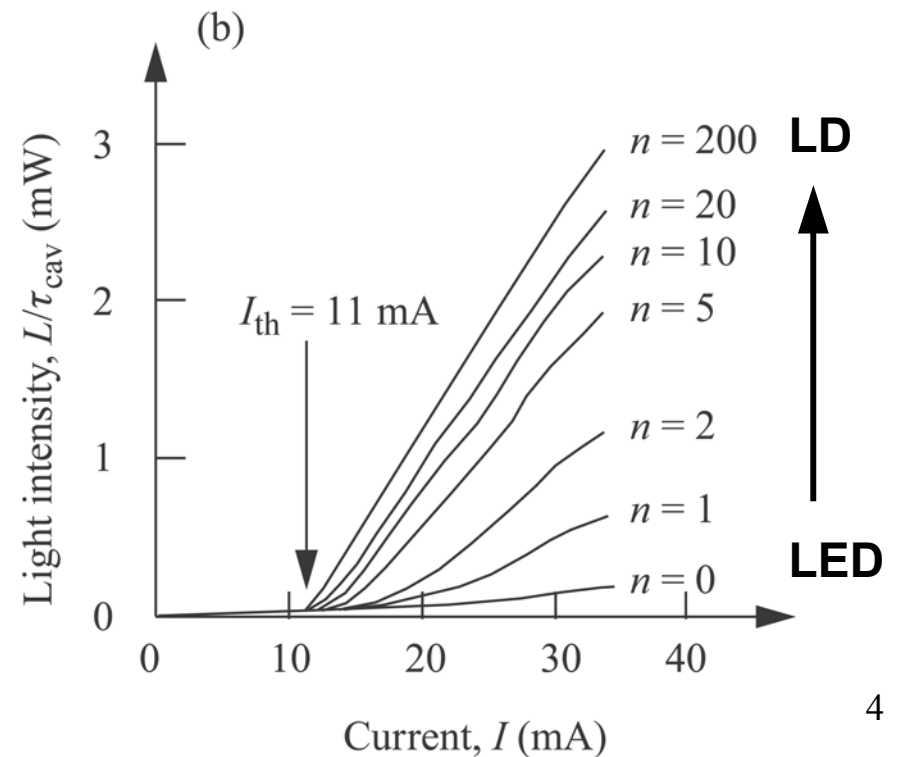
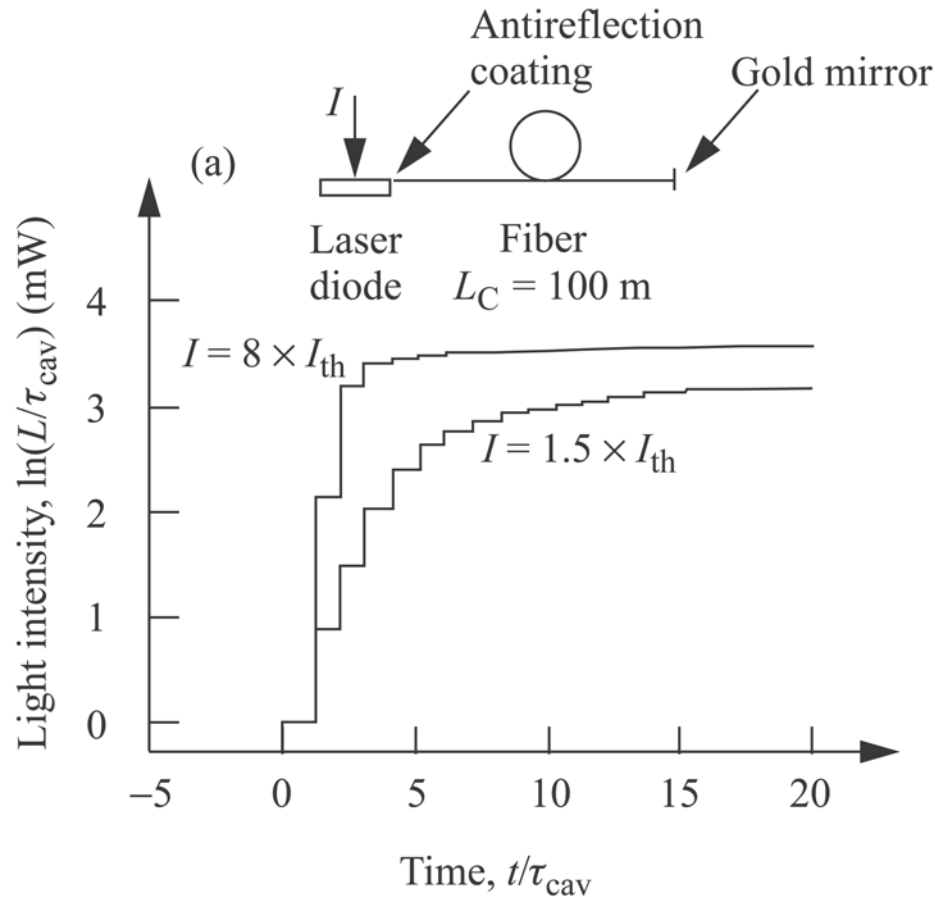
- Photons experience non-linear threshold behavior transitioning from disordered light (spontaneous emission) to ordered light (stimulated emission) with increasing pump current
 - Active volume $300 \times 0.14 \times 0.8 \mu\text{m}^3 = 34 \times 10^{-12} \text{ cm}^{-3} = 34 \mu\text{m}^3$
 - $I_{th} = 3 \text{ mA}$, $\langle n \rangle = 2 \times 10^7$, $\langle s \rangle = 10^5$, $\beta = 10^{-4}$, 7 ps photon cavity round-trip
- Existing mean-field theories (rate equations and Gaussian noise - Langevin) applies to these large systems

Ask a simple question:

When do photons know
they are in a laser?

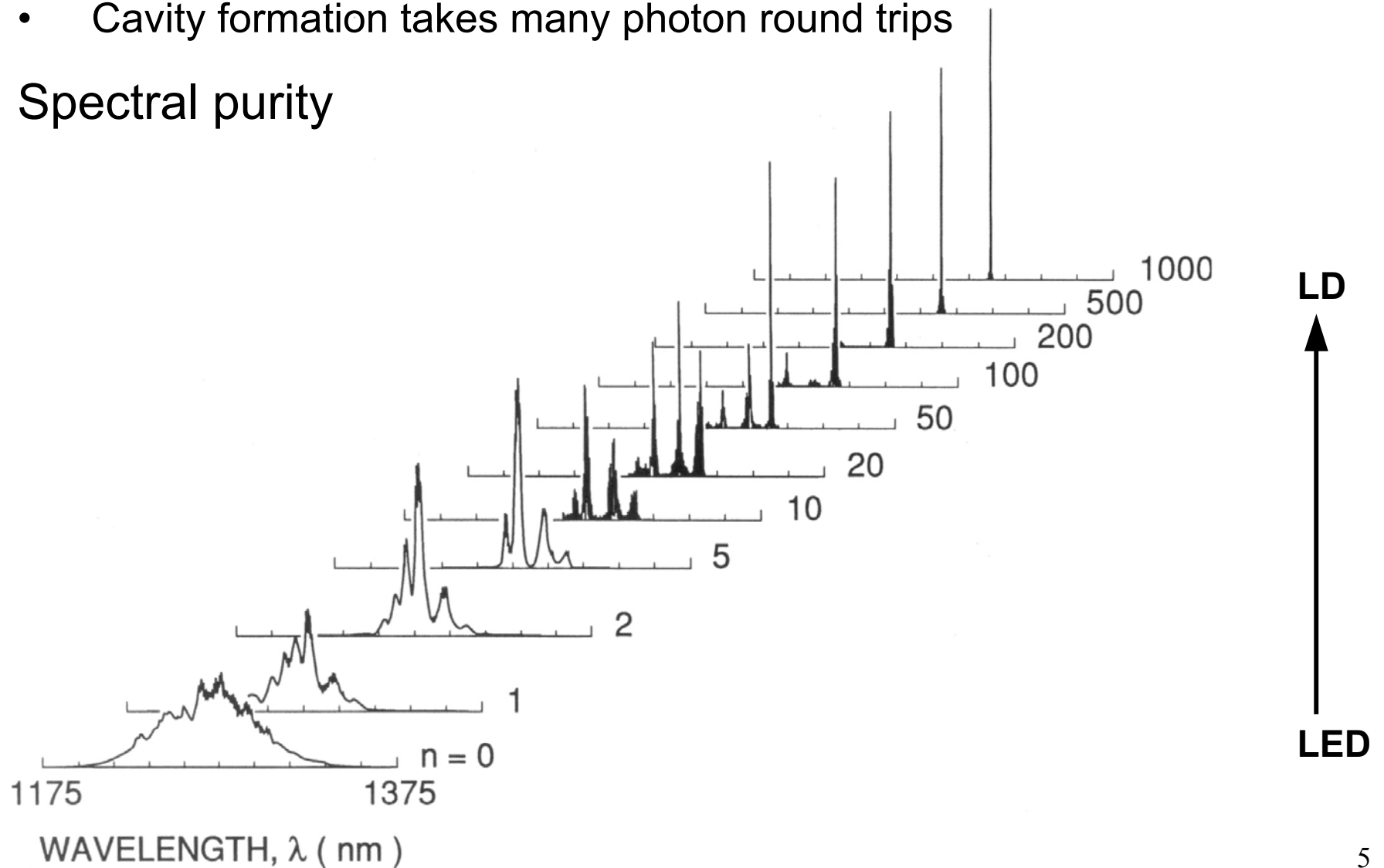
When do photons know they are in a laser?

- NOT one cavity round-trip
 - Cavity formation takes many photon round trips
- Adiabatically decouple electron dynamics in experiment by using large cavity



When do photons know they are in a laser?

- NOT one cavity round-trip
 - Cavity formation takes many photon round trips
- Spectral purity

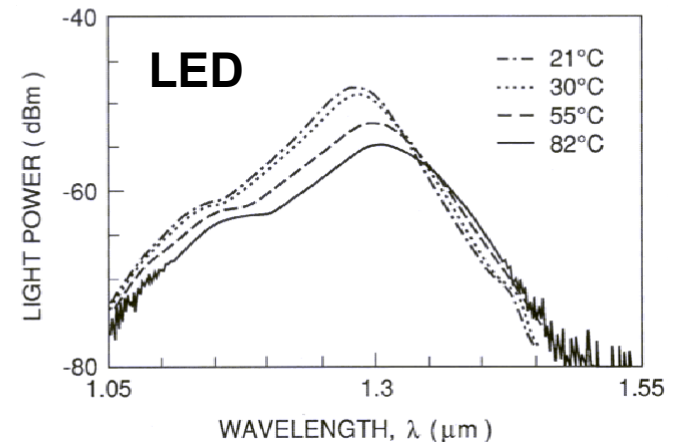
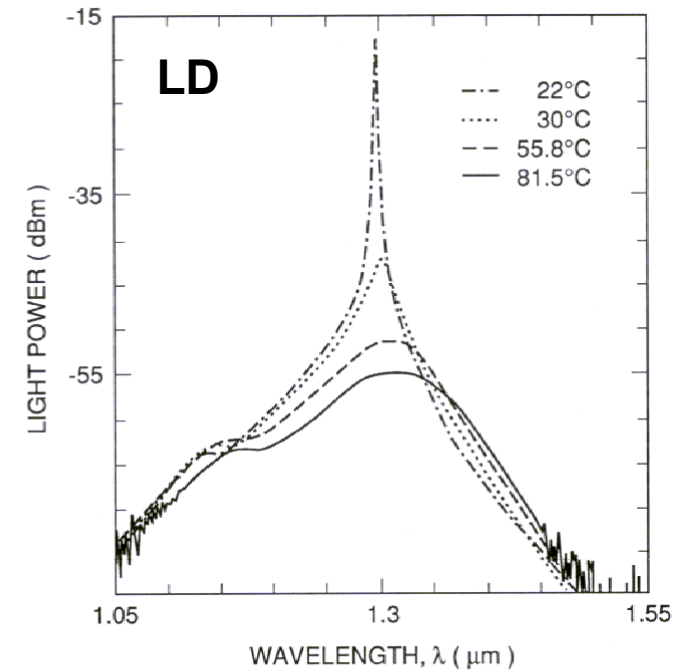
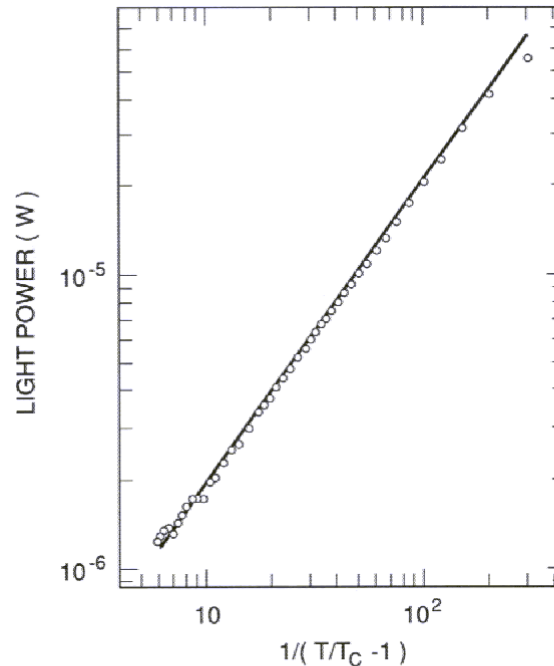


Ask a simple question:

How do photon fluctuations
below threshold impact
lasing emission?

Fluctuations enhance light output below I_{th}

- Experimentally compare LED and LD using SAME geometry and active region
 - AR coat LD to make LED
- Landau-Ginzburg phase transition analogy for bulk with below-threshold fluctuations into the lasing state
 - Intensity fluctuations scale as $1/(T/T_C - 1)^\gamma$
 - Experimentally $\gamma=1.04$, $T_C = 301.4$ K



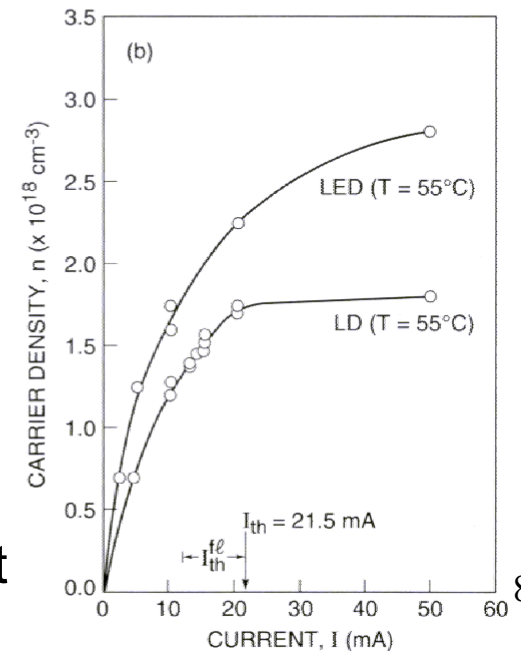
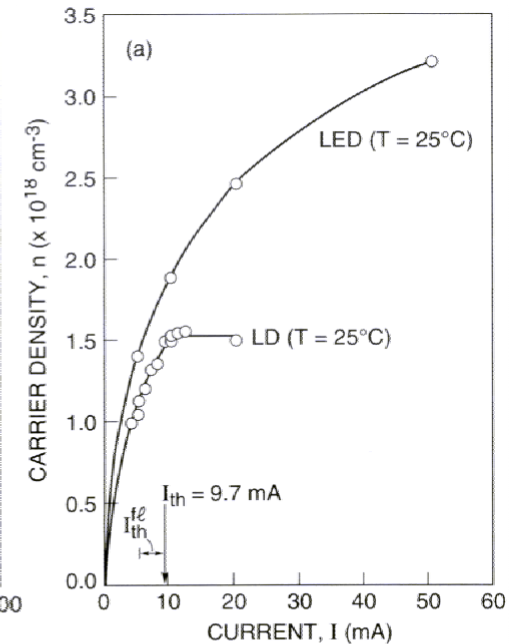
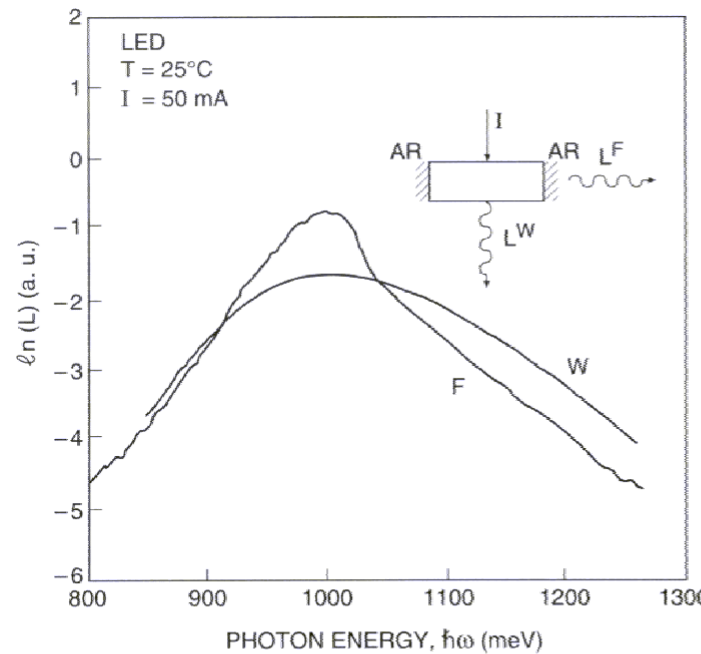
Fluctuations and carrier pinning

- Experimentally compare LED and LD using SAME geometry and active region

- AR coat LD to make LED

- Carrier number n from L_W (spontaneous emission)
- Fluctuations in photons s remove carriers below threshold and contribute to the temperature dependence of laser diode threshold current, I_{th}

- There is a contribution, I_{fl} , to the threshold current



Summary so far:

Photon fluctuations in large laser diodes:

Enhance lasing emission below the threshold current

Remove carriers below the threshold current

Contribute to the temperature dependence of the laser diode threshold current

Photon fluctuations are important !

Fluctuations described by Langevin equations

Single mode, single frequency laser diode rate equations in the presence of noise, F

$$\frac{dn}{dt} = -Gs - \gamma_e n + \frac{I}{e} + F_n(t), \text{ Equation governing carrier number}$$

$$\frac{ds}{dt} = (G - \kappa)s + \beta R_{sp} + F_s(t), \text{ Equation governing photon number}$$

$$G = a\Gamma(v_g / n_r)(n - n_g) / V, \text{ expression for gain}$$

$$R_{sp} = Bn^2 / V, \text{ expression for spontaneous emission}$$

Correlation of noise sources:

$$\langle F_s(t)F_s(t') \rangle = V_{ss} \delta(t-t') = [[G + \kappa]s + \beta R_{sp}] \delta(t-t')$$

$$\langle F_n(t)F_n(t') \rangle = V_{nn} \delta(t-t') = [Gs + \gamma_e n + \frac{I}{e}] \delta(t-t')$$

$$\langle F_s(t)F_n(t') \rangle = 0$$

$\delta(t-t')$ Ensures Markovian noise

Noise in particle number introduced by addition of external Gaussian noise – method valid only in large particle number (thermodynamic) limit

γ_e = Carrier recombination rate

B = Radiative recombination rate

I = Injection current

e = Electronic charge

n = Number of electrons in cavity

s = Photon number in the cavity

a = Gain slope coefficient

Γ = Mode confinement factor

L = Length of cavity

n_g = Carrier number at transparency

v_g = Velocity of light

n_r = refractive index

$r_{1,2}$ = reflectivity of mirror 1,2

α_i = internal loss

$\alpha_m = \frac{1}{2L} \log(\frac{1}{r_1 r_2})$, loss due to mirrors

$\kappa = (\alpha_i + \alpha_m)(\frac{v_g}{n_r})$, Loss rate in the

cavity

V = Volume of cavity

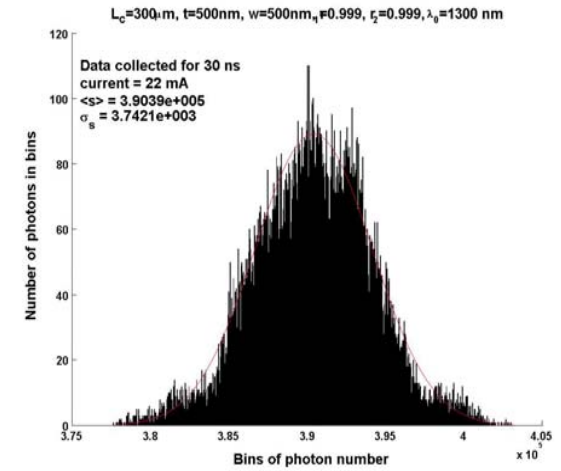
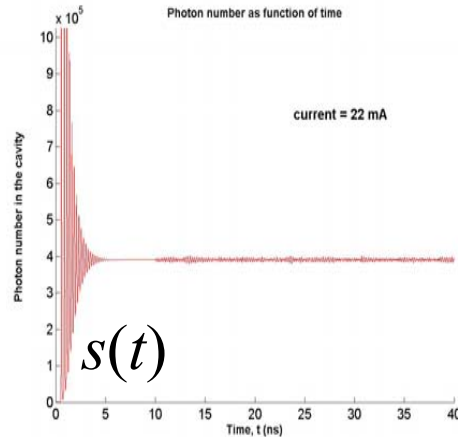
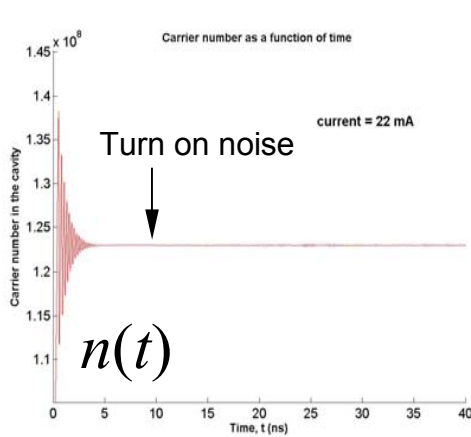
$F_n(t)$ = Random noise in carrier number

$F_s(t)$ = Random noise in photon number

Simulations of large and small laser diode using Langevin equations

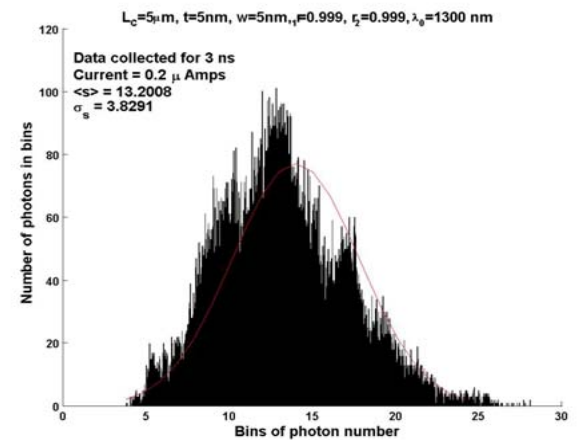
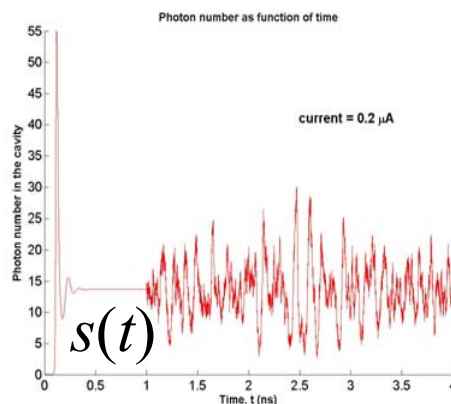
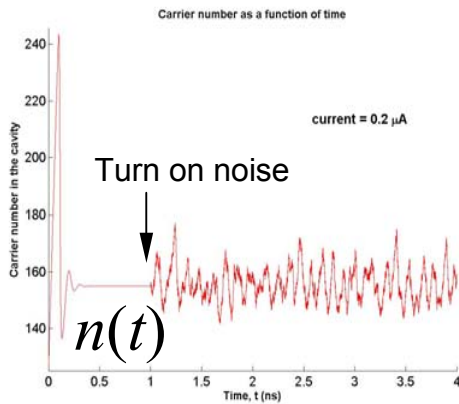
Results for large cavity: Volume = $75\mu\text{m}^3$, $\Gamma = 0.25$, $a = 2.5\text{e-}016\text{ cm}^2/\text{s}$, $B = 1\text{e-}010\text{cm}^3/\text{s}$, $\beta = 1\text{e-}04$, $n_g = 1\text{e+}18/\text{cm}^3$, $\alpha_1 = 40\text{cm}^{-1}$

$$n_r = 4, \langle s \rangle = 3.9039\text{e+}005, \sigma_s = 3.7421\text{e+}003, I_{\text{th}} = 3.25\text{mA}$$



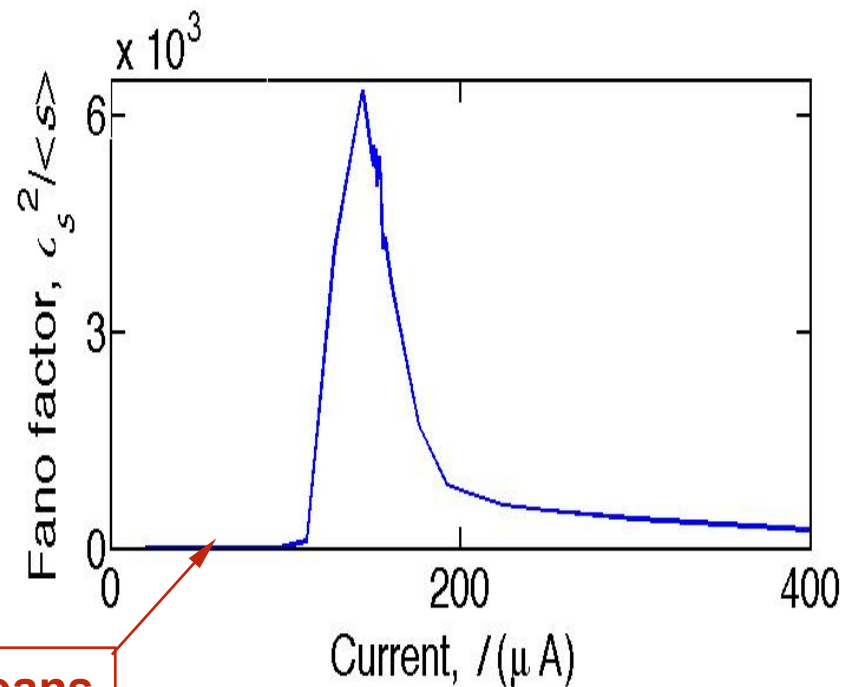
Results for small cavity: Volume = $1.25\text{e-}4\mu\text{m}^3$, $\Gamma = 0.1$, $a = 5\text{e-}016\text{ cm}^2/\text{s}$, $B = 1\text{e-}010\text{cm}^3/\text{s}$, $\beta = 1\text{e-}04$, $n_g = 1\text{e+}18/\text{cm}^3$, $\alpha_1 = 10\text{cm}^{-1}$

$$n_r = 4, \langle s \rangle = 13.2008, \sigma_s = 3.8291, I_{\text{th}} = 3\text{ nA}$$



Characterizing fluctuations: The Fano-factor

- Fano-factor = $\sigma_s^2 / \langle s \rangle = (\langle s^2 \rangle - \langle s \rangle^2) / \langle s \rangle$ measures the strength in photon fluctuations
- Peaks sharply across threshold if a threshold exists and the system undergoes a phase transition
- For Poisson fluctuations $\sigma_s^2 / \langle s \rangle = 1$



**Fano factor = 1, means
Poisson fluctuations**

Previous work – quantum theory

- In a **full quantum statistical approach** both the **medium** and **light** is **quantized**
- This treatment of lasers can be broadly classified into **two** categories:
 - A **phase-space description** in terms of **Fokker-Plank equations** by Haken, which accounts for the small fluctuations in the system about the mean
 - Only calculated for large systems with small fluctuations
 - The **density matrix description** of Scully and Lamb
 - Only calculated for large systems with small fluctuations
- Theories are complete in the sense that they provide information about **particle statistics** and laser **line width**, but, in practice, they have only been solved for **large systems**

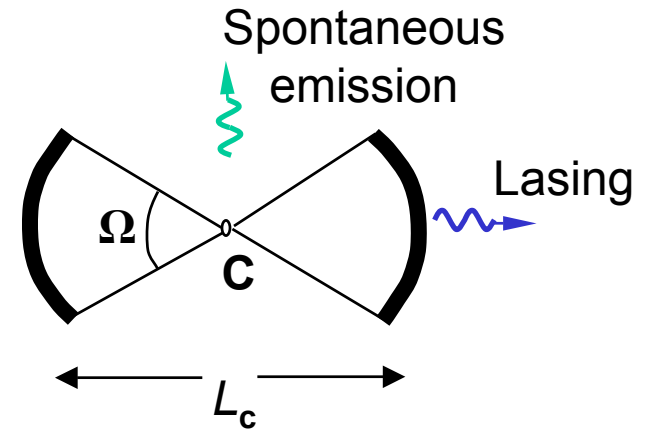
Ask a simple question:

How do small laser diodes
behave?

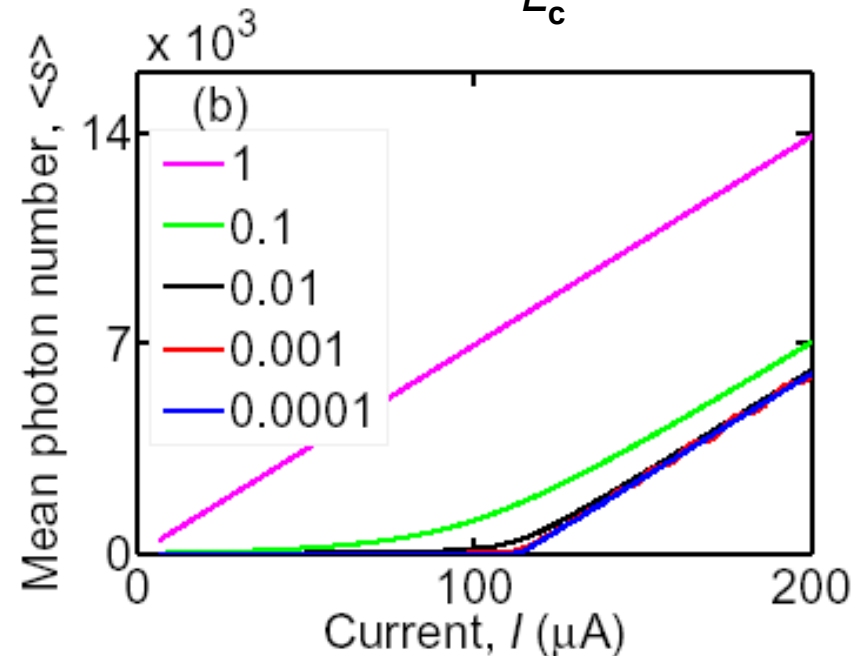
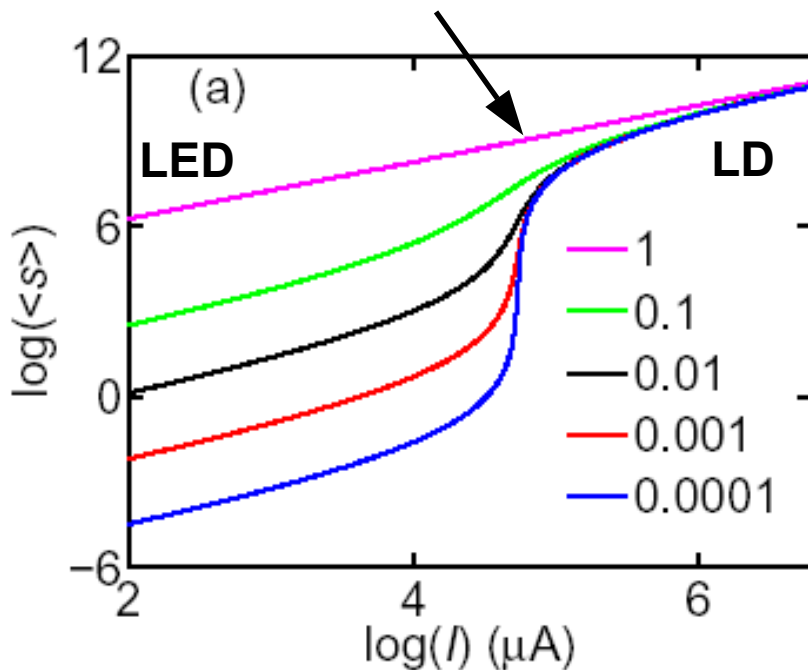
What happens when a laser is made small?

- More spontaneous emission into lasing mode, $\beta \sim 0.1$
- Continuum mean-field rate equations predict “soft” threshold
 - Active volume $0.12 \times 10^{-12} \text{ cm}^{-3} = 0.12 \mu\text{m}^3$
 - $I_{\text{th}} < 1 \text{ mA}$, $\langle n \rangle = 2 \times 10^5$, $\langle s \rangle = 10^3$

$$\beta = \Omega/4\pi \longrightarrow L_c (\longrightarrow 0), \Omega (\longrightarrow 4\pi), \beta (\longrightarrow 1)$$

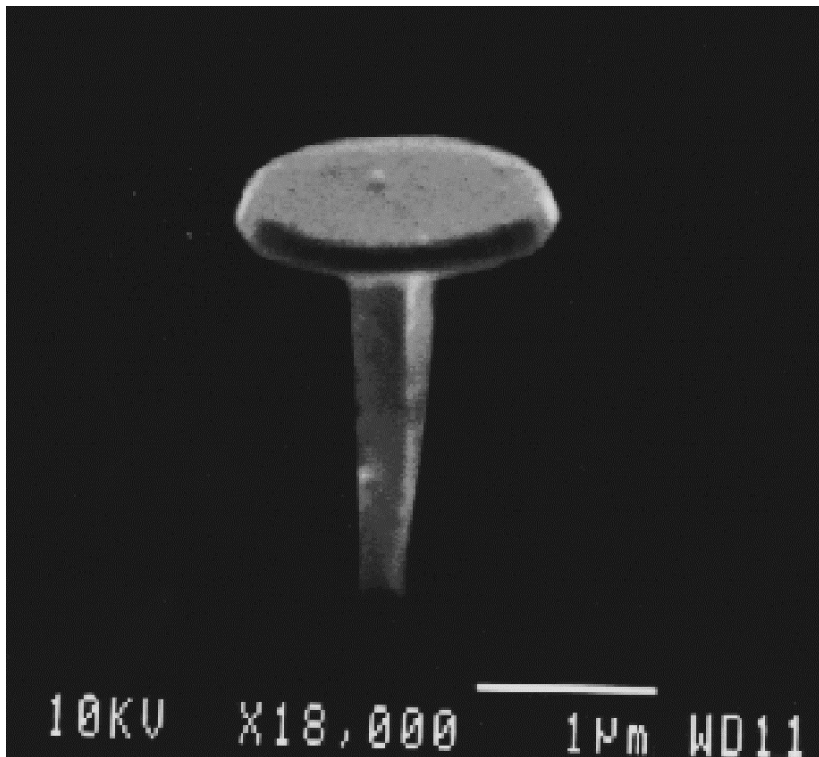


“Thresholdless” lasing

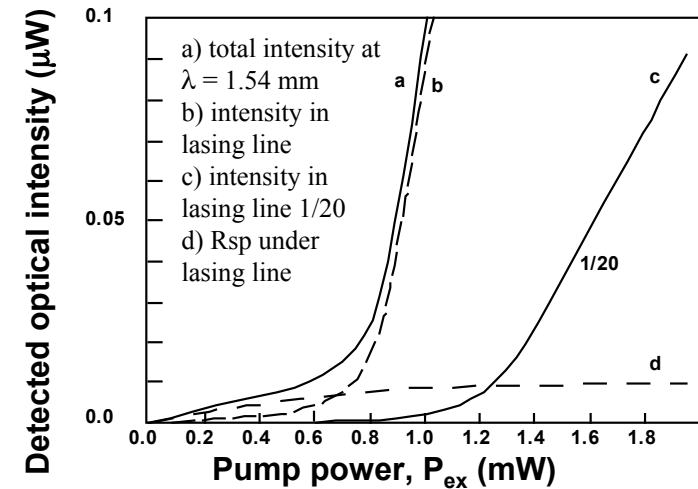


What happens when a laser is made small?

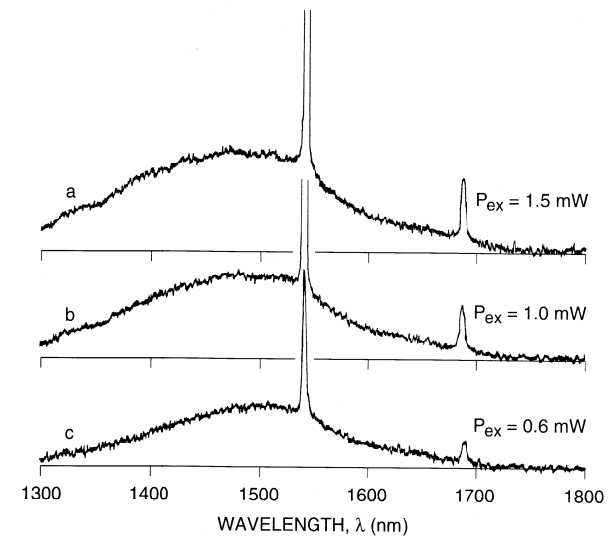
- More spontaneous emission into lasing mode, $\beta \sim 0.1$
- Fluctuations more important
 - Active volume $0.12 \times 10^{-12} \text{ cm}^{-3}$
 - $I_{th} < 1 \text{ mA}$, $\langle n \rangle = 2 \times 10^5$, $\langle s \rangle = 10^3$



6-QW microdisk laser, $R = 0.8 \mu\text{m}$, $h = 0.18 \mu\text{m}$



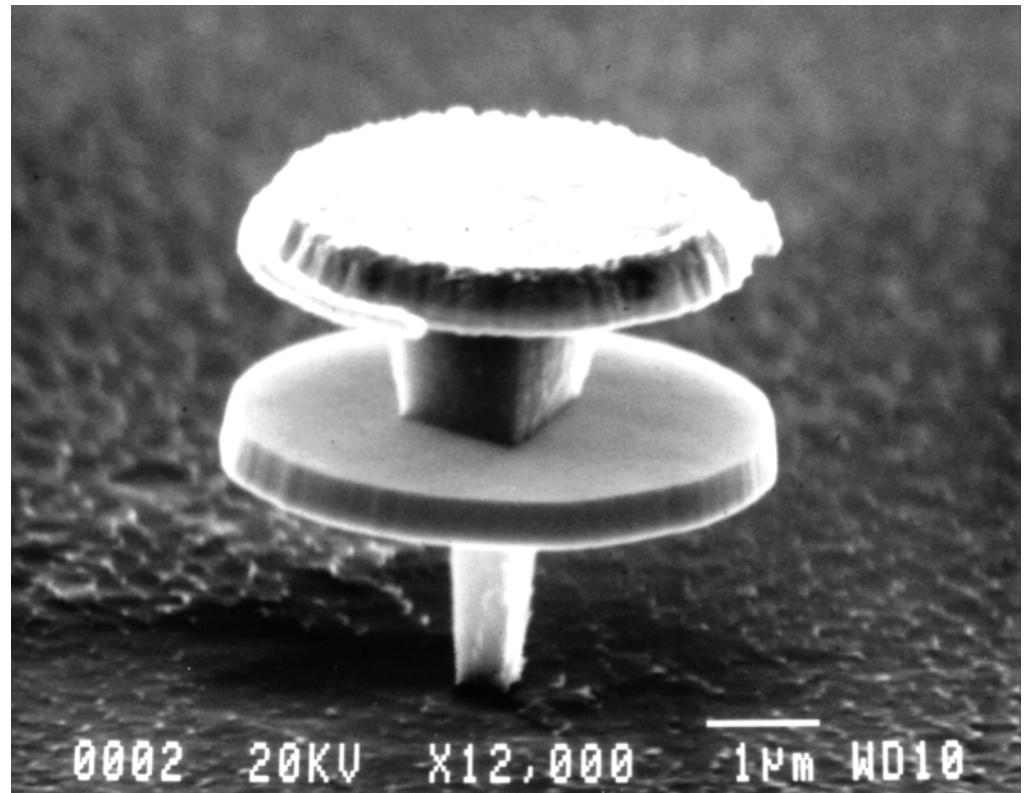
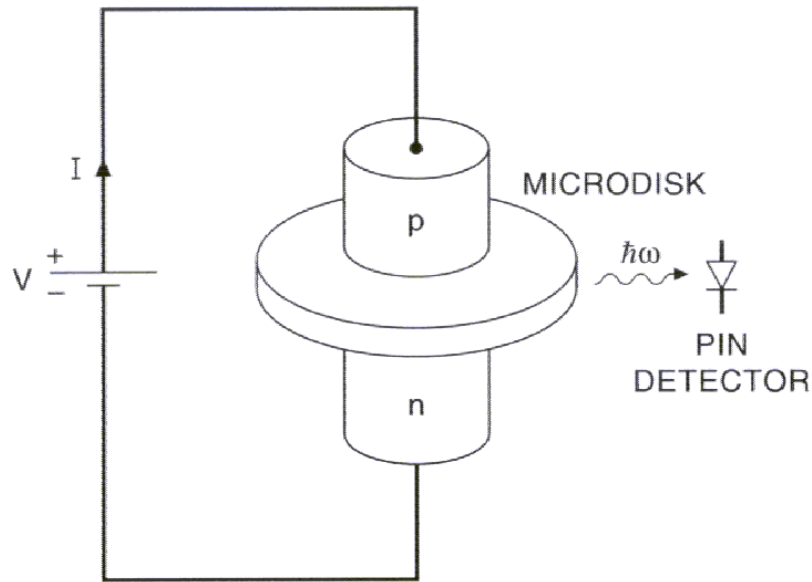
Optically pumped 6-QWs microdisk laser input-output characteristics



Room temperature emission spectra mode spacing $\Delta\lambda = 1690-1542 = 148 \text{ nm}$

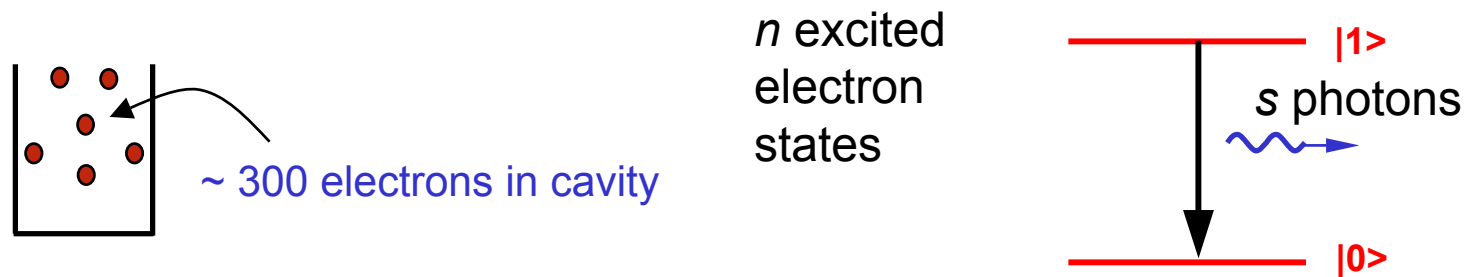
Electrically driven microdisk laser diode

- Small active and cavity volume



Quantum fluctuations in a *very* small laser

- Small active and cavity volume
 - Small electron number, n , and photon number, s



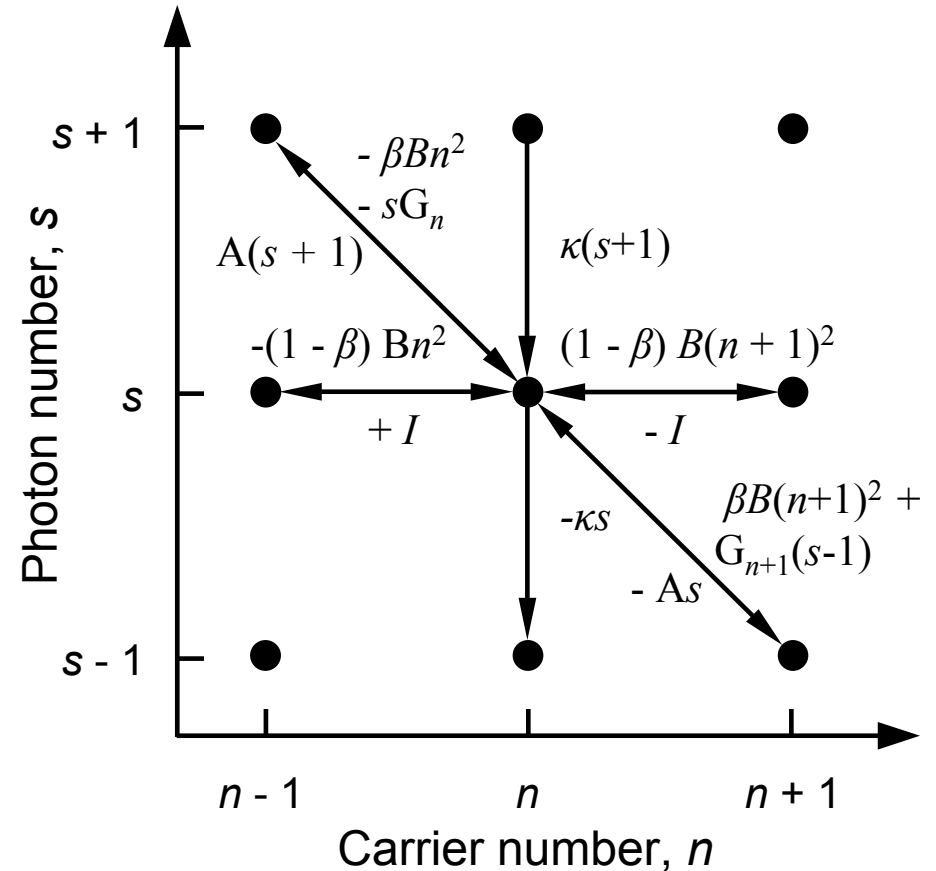
- Fluctuations ($\langle s^2 \rangle$ and $\langle n^2 \rangle$) and correlations ($\langle ns \rangle$) in particle number become important
- Mean-field theories (rate equations and Gaussian noise - Langevin) can not be used
- What effect do large fluctuations and strong correlations have on steady-state and temporal behavior of small lasers in the quantum regime?

Quantum fluctuations in a *very* small laser

- Solving the full quantum mechanical problem is difficult at the meso-scale because the number of system states can become very large
 - Small electron number, n (~ 300), and small photon number, s (~ 100)
 - The number of system states scales as $(2^n) \times s$, where n is the number of two-level electronic states and s is the number of photons in the lasing mode
 - The corresponding coefficient matrix has size $(2^n)s \times (2^n)s$ and so the problem becomes computationally challenging with increasing number of electronic states inside the cavity
 - For only 20 two-level electronic states and 100 photons $(2^n) \times s$ is state vector of length about 10^8 (note $(2^{300}) \times 100 \sim 2 \times 10^{92}$ which is more than the number of atoms in the universe)
- Need a different approach

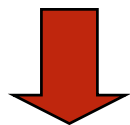
Master equations

- First-cut at capturing quantum effects
 - Photon energy $\hbar\omega$
 - Quantize photon number s and excited electron particle number n
 - Weak coupling
- Use master equations (a set of differential equations in continuous probability functions, P_{ns}) to describe the system



$$d\langle n \rangle / dt = I - B\langle n^2 \rangle - a\Gamma\langle n - n_0 \rangle \langle s \rangle / V$$

$$d\langle s \rangle / dt = \beta B\langle n^2 \rangle + a\Gamma\langle n - n_0 \rangle \langle s \rangle / V - \kappa\langle s \rangle$$



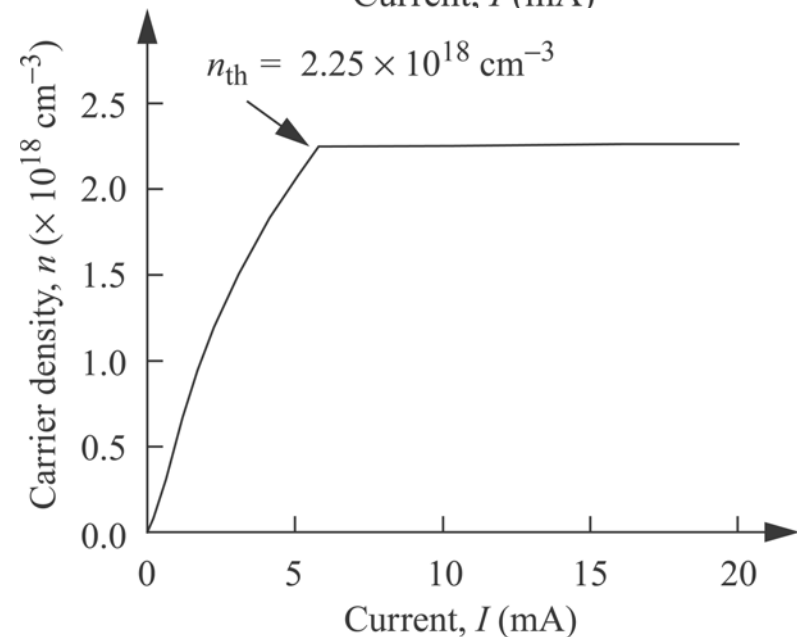
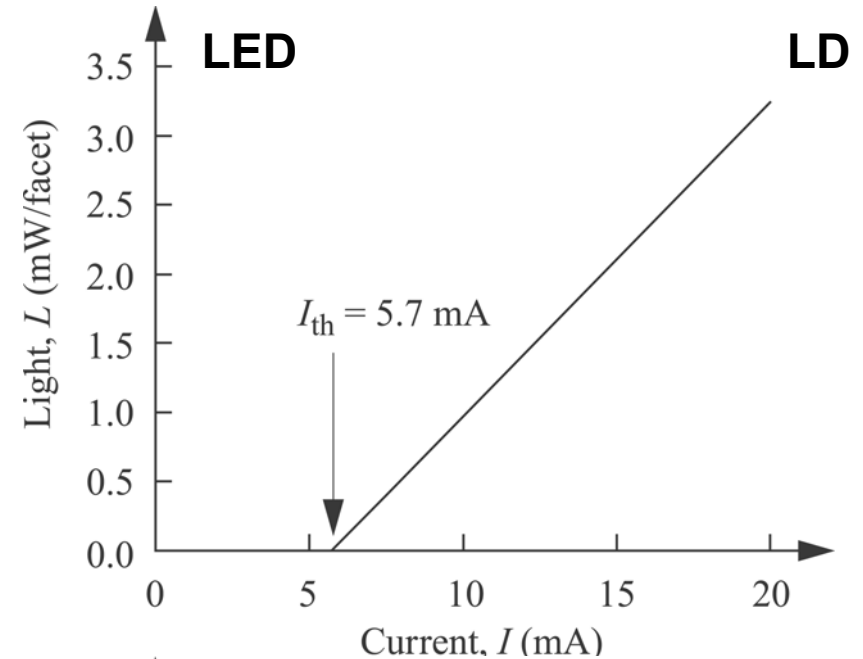
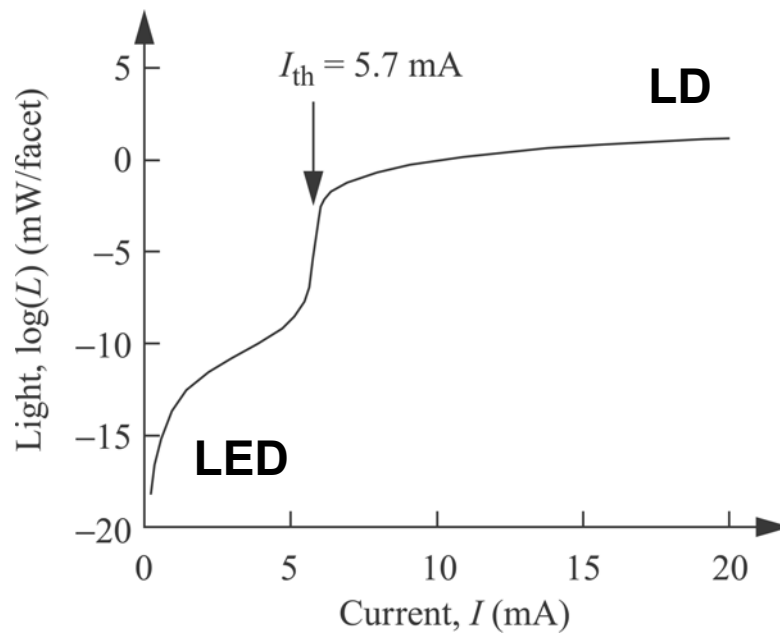
Continuum mean-field rate equations set $\langle ns \rangle = \langle n \rangle \langle s \rangle$
 Master equations, $\langle ns \rangle \neq \langle n \rangle \langle s \rangle$

$$\frac{dP_{n,s}}{dt} = -\kappa(sP_{n,s} - (s+1)P_{n,s+1}) - (sG_n P_{n,s} - (s-1)G_{n+1} P_{n+1,s-1}) - (sAP_{n,s} - (s+1)AP_{n-1,s+1})$$

$$- \beta B(n^2 P_{n,s} - (n+1)^2 P_{n+1,s-1}) - (1-\beta)B(n^2 P_{n,s} - (n+1)^2 P_{n+1,s}) - I(P_{n,s} - P_{n-1,s})$$

Continuum mean-field rate equation prediction

- Steady-state behavior predicted by continuum mean-field rate equations
 - Threshold** current I_{th}
 - Carrier number n **pinned** when $I > I_{th}$



Continuum mean-field rate equation prediction

- Why carriers are pinned above I_{th}

In steady-state

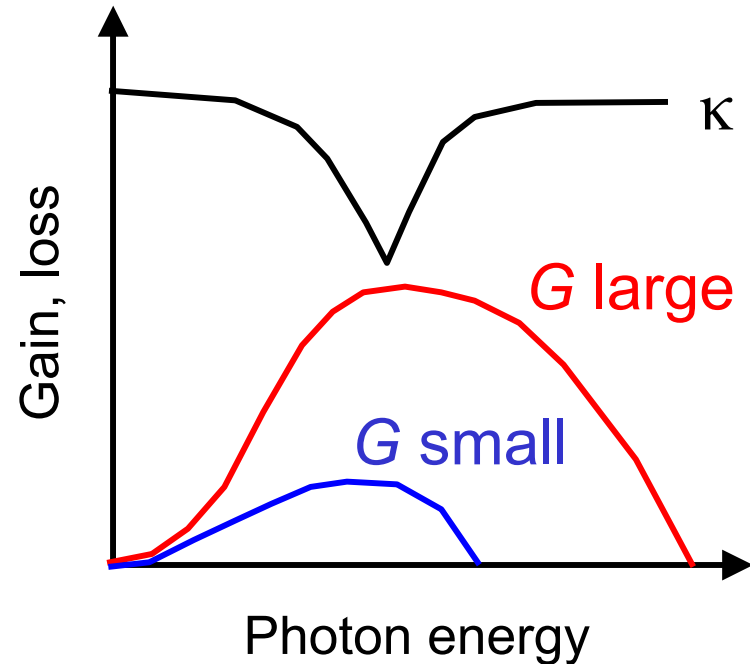
$$\frac{dn}{dt} = \frac{I}{e} - \gamma_e n - Gs = 0$$

$$\frac{ds}{dt} = (G - \kappa)s + \beta R_{sp} = 0$$

and

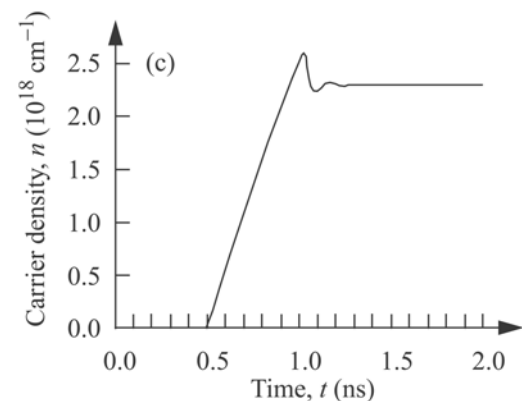
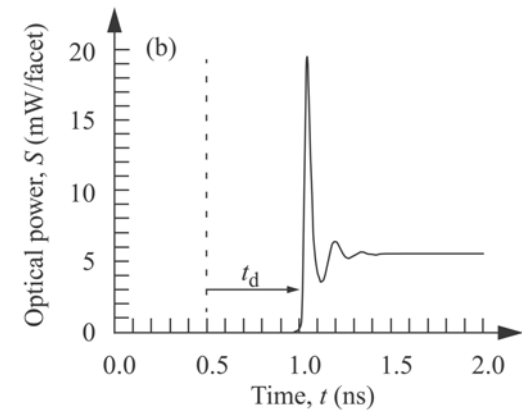
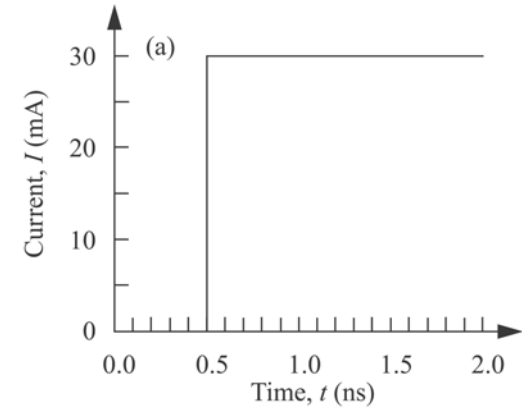
$$s = \frac{\beta R_{sp}}{(\kappa - G)}$$

As $G \rightarrow \kappa$ the number of photons in the system increases rapidly and Gs becomes large, so every extra electron injected into the system is converted into a photon, pinning the carrier density, n

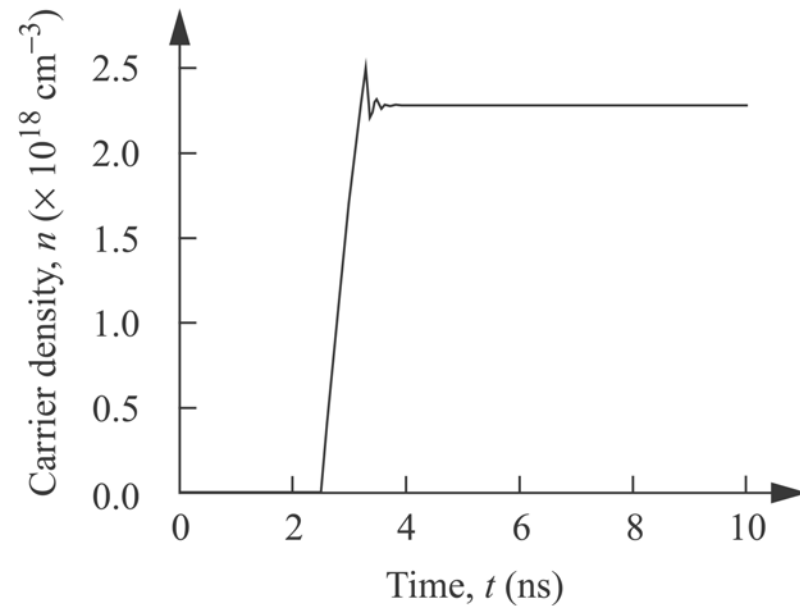
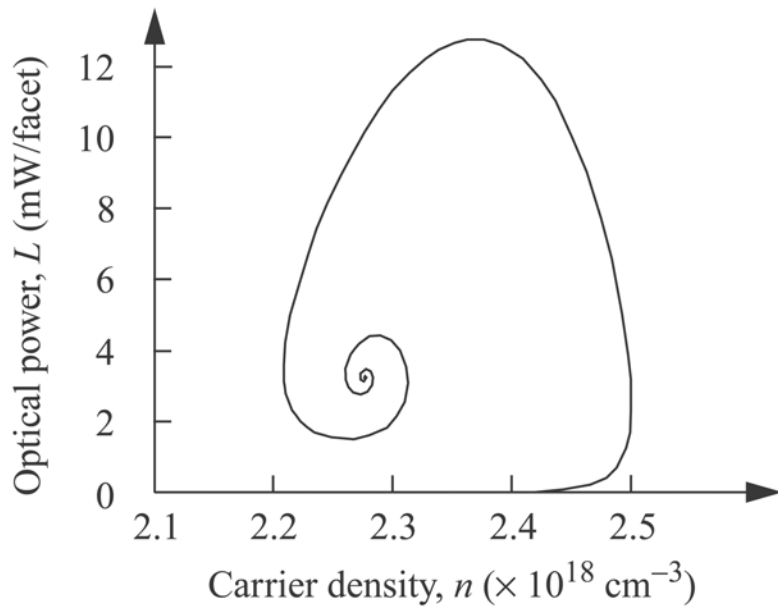
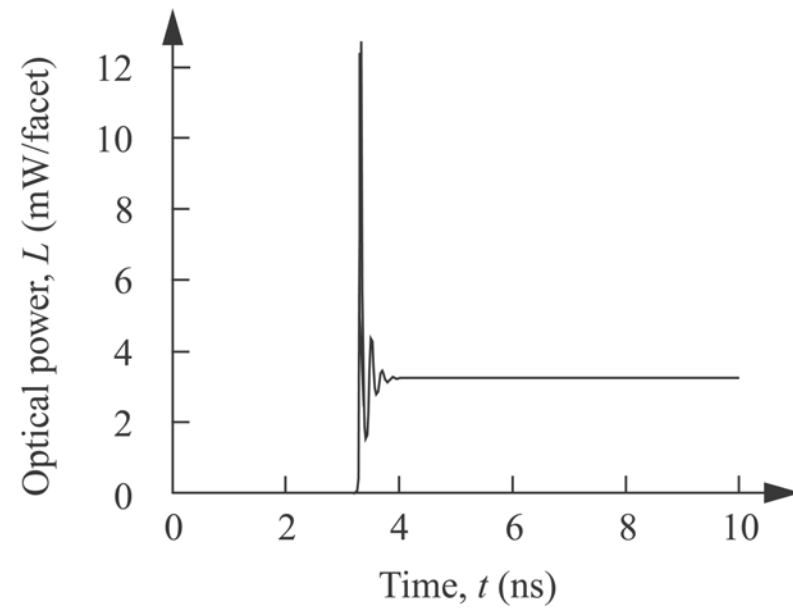
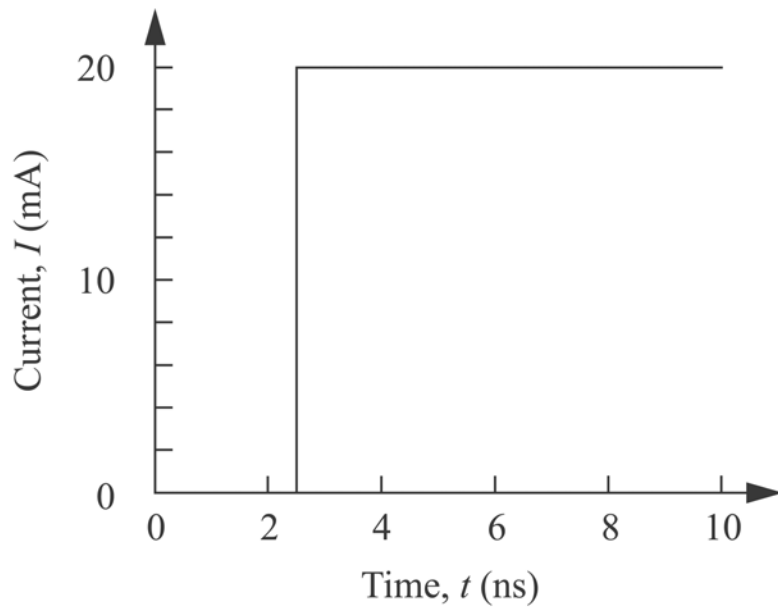


Continuum mean-field rate equation prediction

- Continuum mean-field rate equations predicted transient response to step change in current
 - Initial current $I = 0$ mA
 - Initial carrier number $n = 0$
- Light output
 - Turn-on delay, t_d
 - Relaxation oscillation
- Carrier density
 - n leads s
 - Overshoot
 - Relaxation oscillation



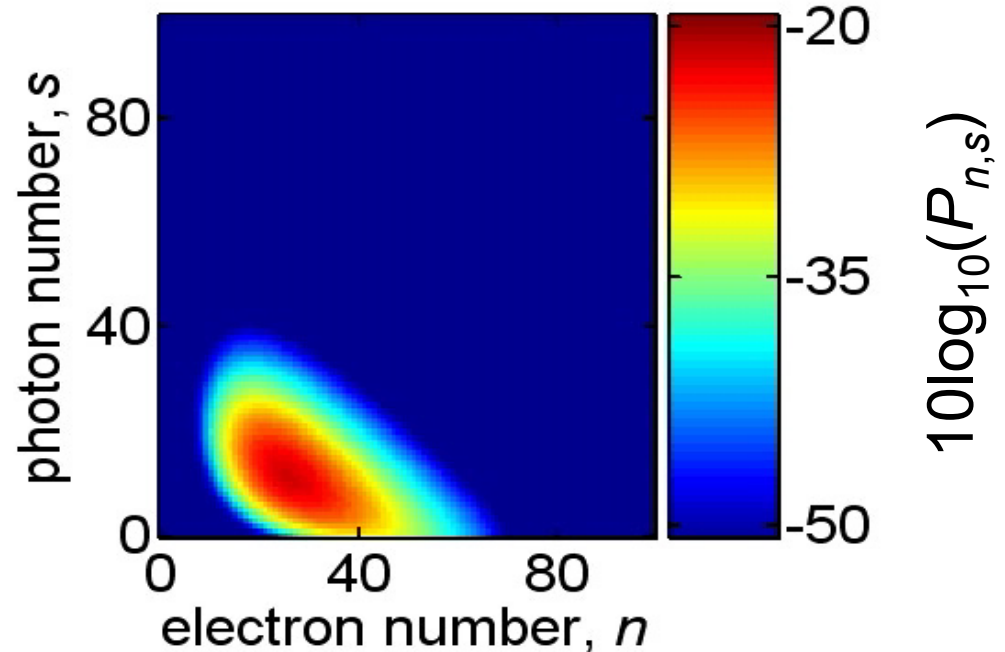
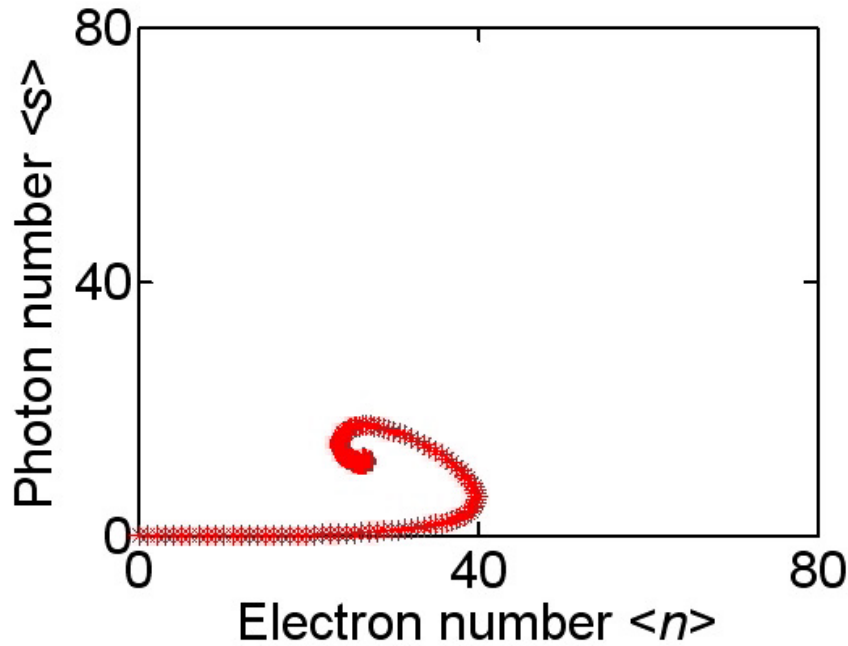
Continuum mean-field rate equation prediction



Mean-field versus probabilistic picture

Continuum mean-field rate equation (R.E.) prediction

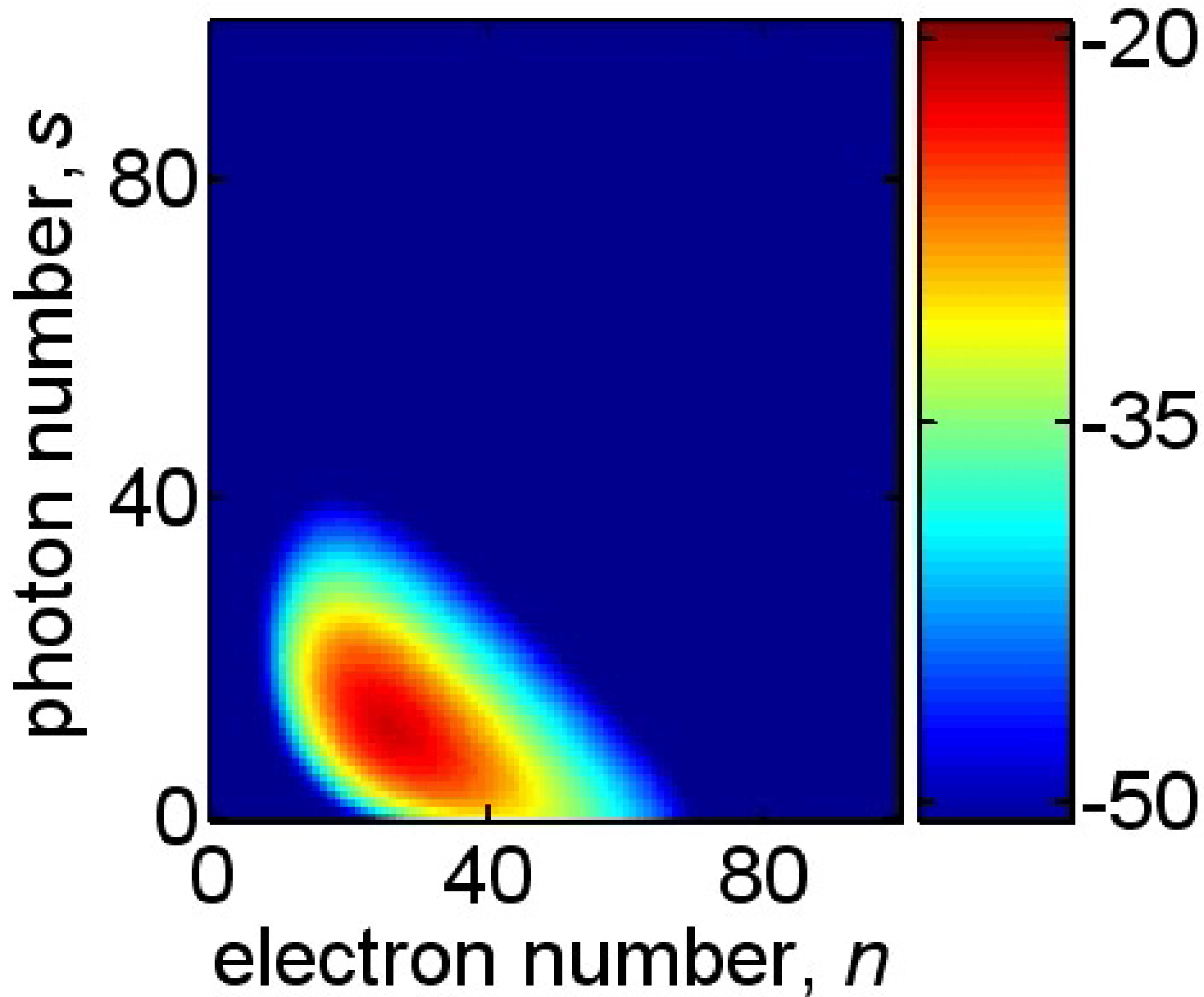
Modeling discrete quantum system using continuum probability functions



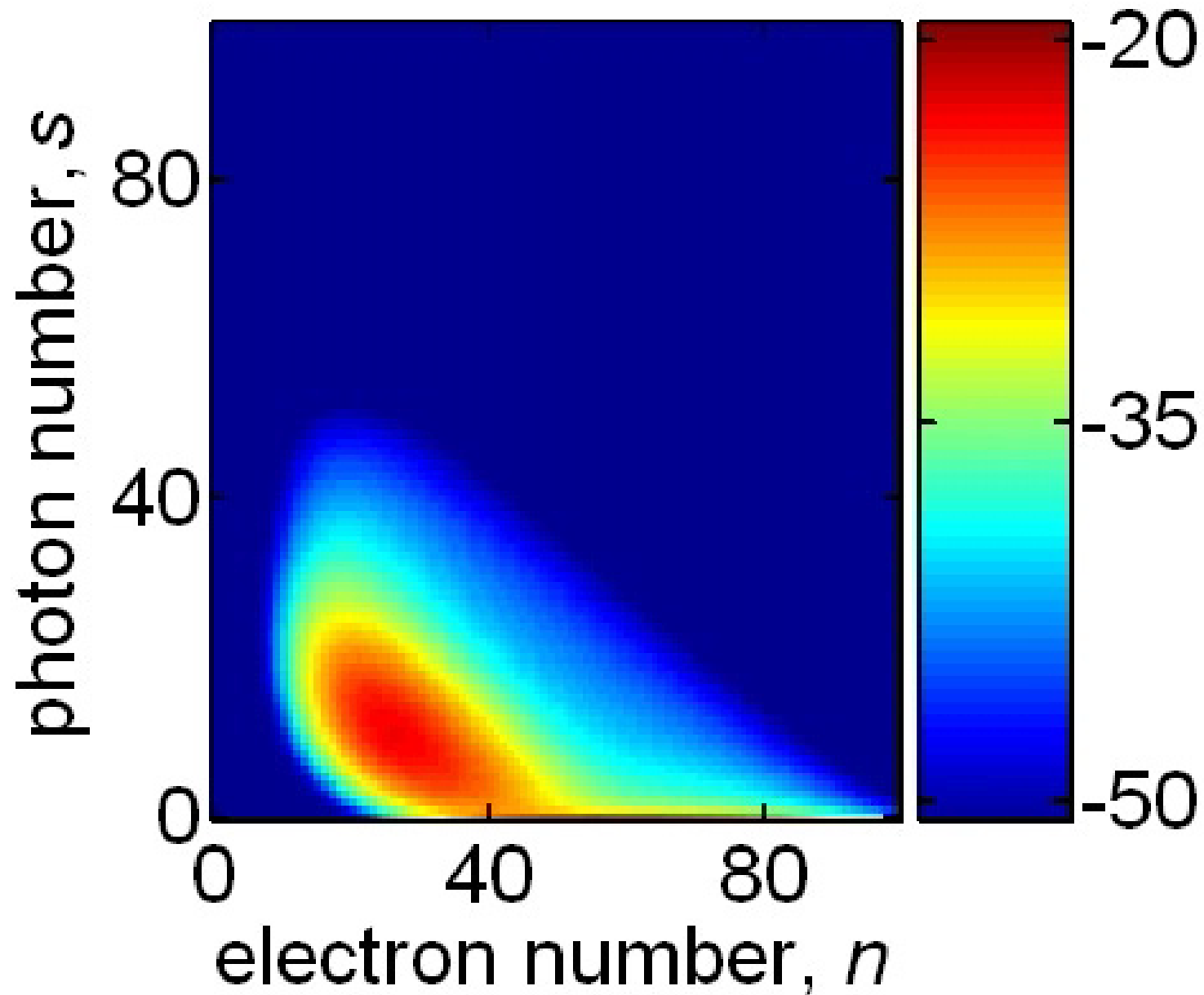
Approximate first moment ($\langle n \rangle$, $\langle s \rangle$) continuum mean – field calculation

Probabilistic picture, $P_{n,s}$ for n electrons and s photons in the cavity

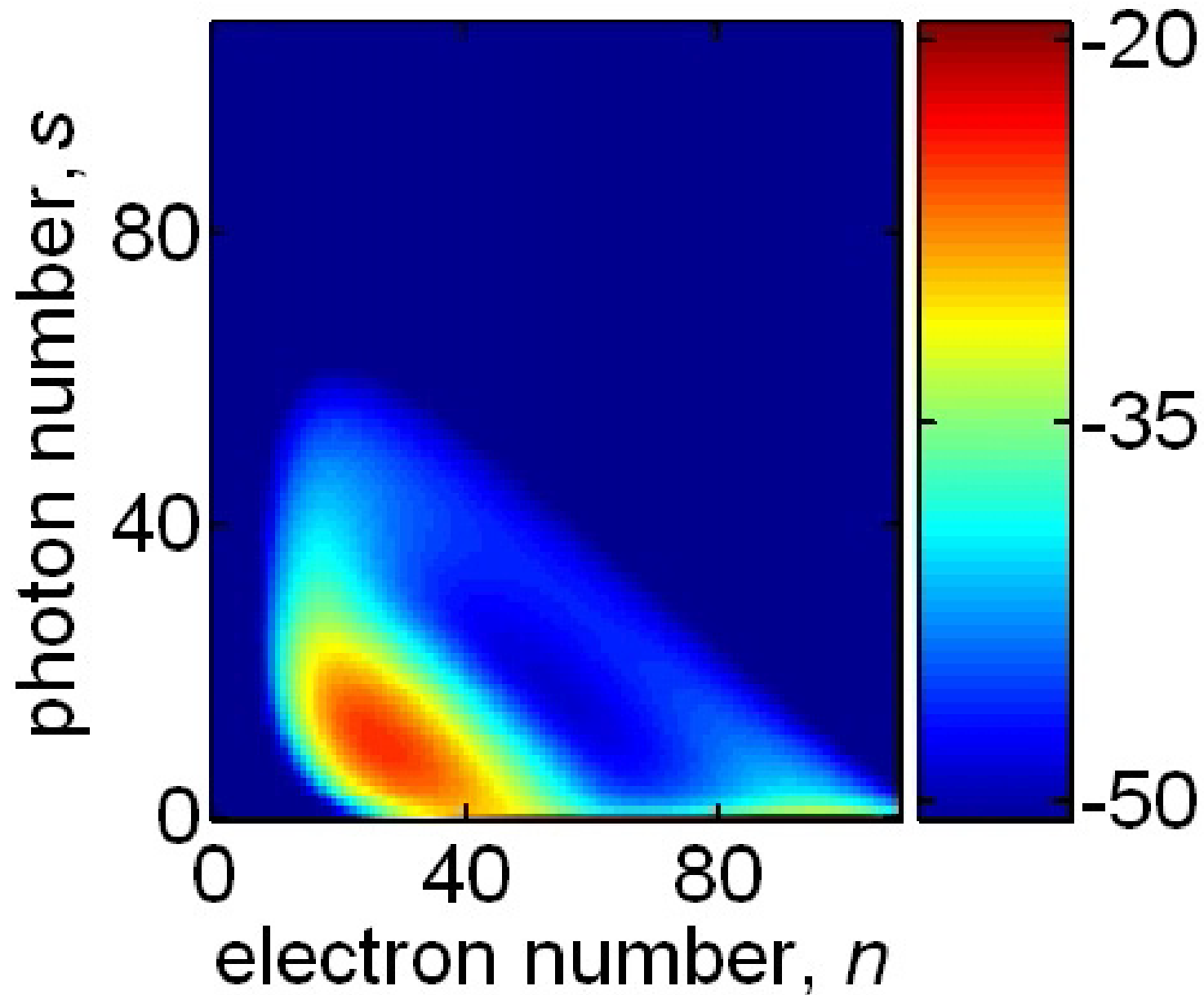
Time evolution of $10\log_{10}(P_{ns})$ for $\beta=1$



Time evolution of $10\log_{10}(P_{ns})$ for $\beta=0.1$



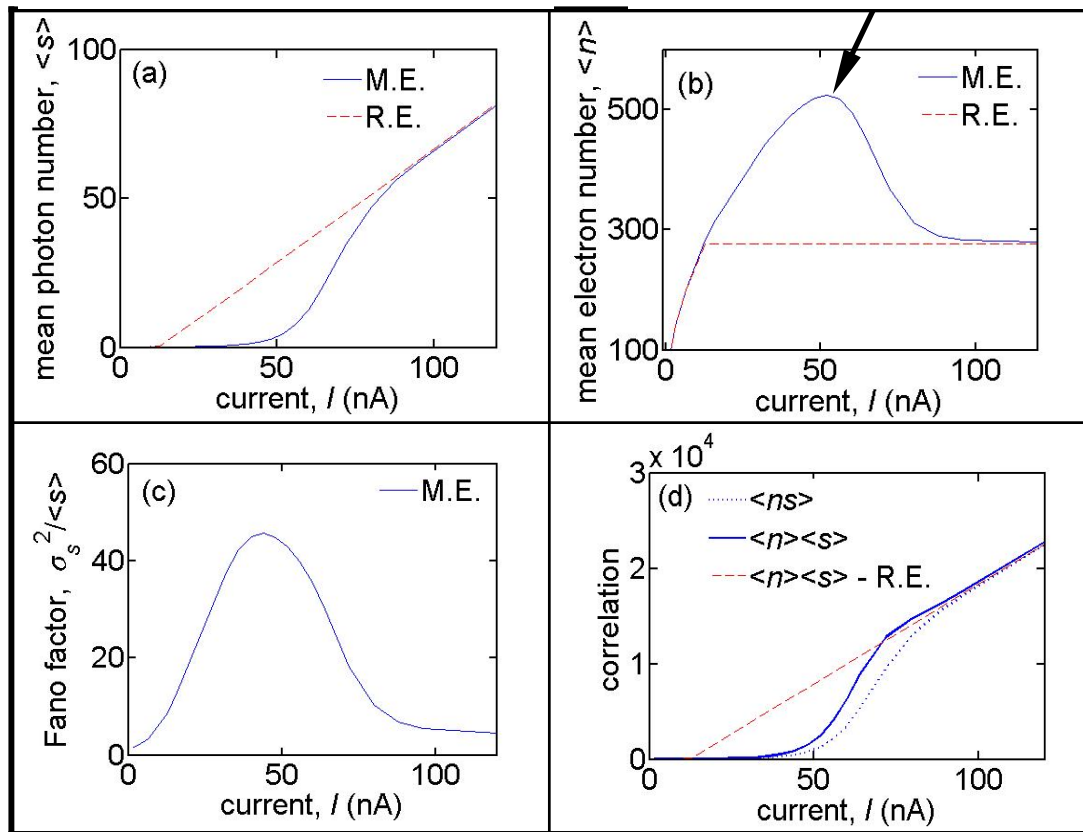
Time evolution of $10\log_{10}(P_{ns})$ for $\beta=0.01$



Master equation predictions for small cavity

Suppression of
lasing
due to fluctuations

De-pinning of
carriers



$\langle ns \rangle$ does not factorize ($\langle n \rangle \langle s \rangle$) in the **small cavity** limit leading to **suppression** of lasing and **de-pinning** of carriers.

Parameters : Volume = $0.1 \mu\text{m} \times 0.1 \mu\text{m} \times 10 \text{nm}$, $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$, $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-4}$, $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$, $r = 1 - 10^{-6}$.

Figure . (a) $I = 9.6 \text{ nA}$. (b) $I = 48 \text{ nA}$. (c) $I = 72 \text{ nA}$. (d) $I = 192 \text{ nA}$.

Summary so far for small lasers:

Fluctuations more important in small devices:

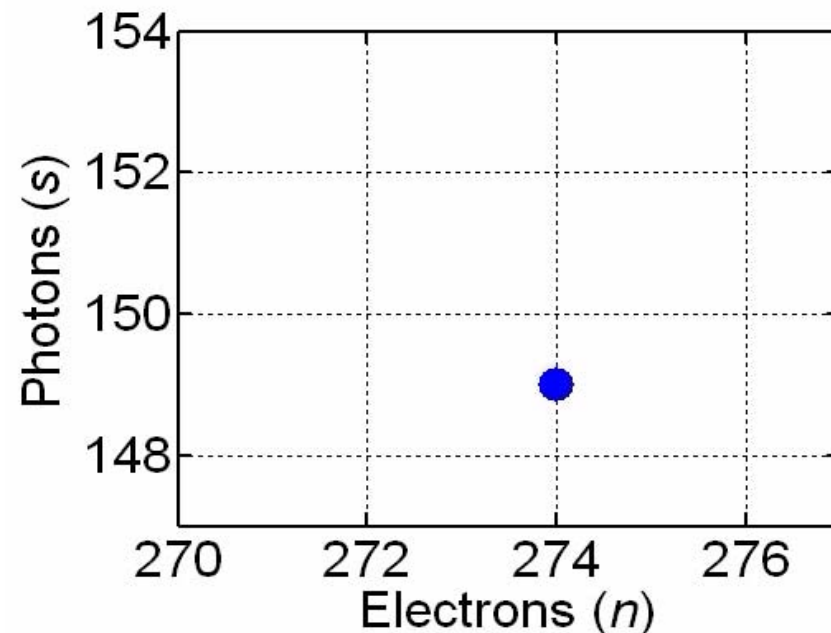
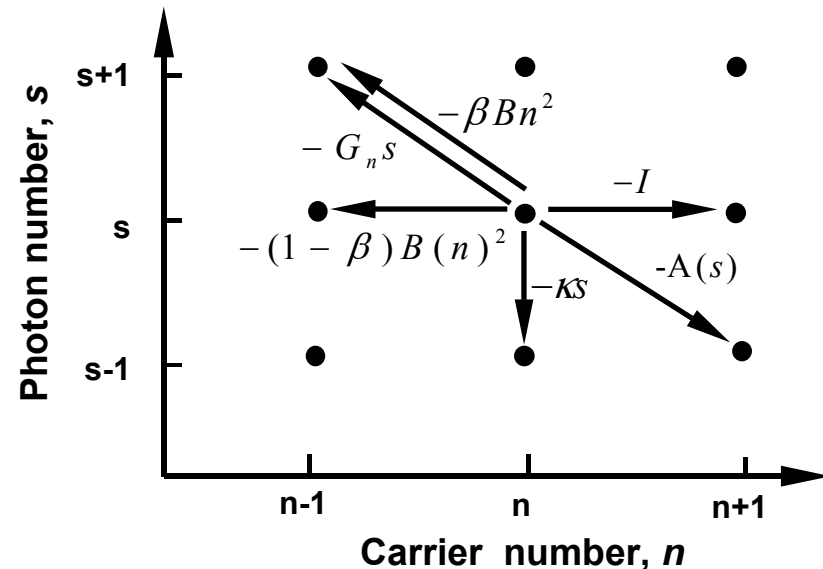
Master equations used to model discrete quantum system using continuum probability functions, P_{ns}

Predict suppression of lasing and de-pinning of carriers due to fluctuations (contrary to expectations of continuum mean-field rate equations)

Need a different approach to understand the origin of these predictions (e.g. plot quantum trajectory)

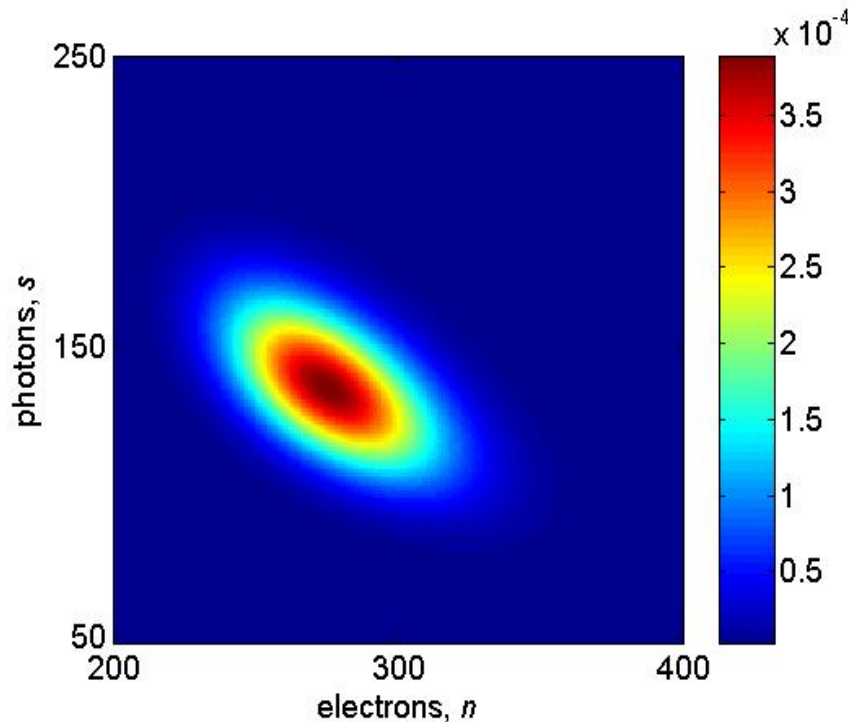
Laser simulation by Monte Carlo method

- At time t , system in state (n, s) has a choice to participate in six independent processes
- The time constants for different processes at time t , is estimated using the rate equation rates, e.g. photon cavity decay rate is $(\tau_{\text{decay}} = 1/ \kappa S)$
- System allowed to perform random walk on a 2D grid

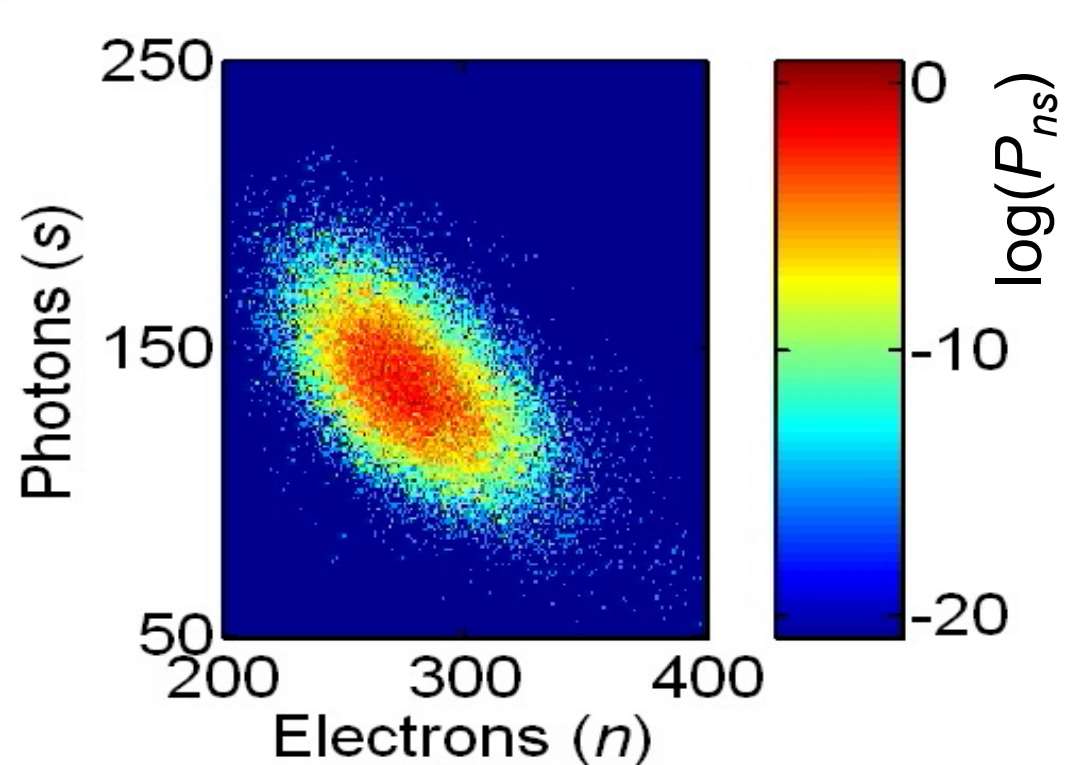


Laser simulation by Monte Carlo method

- Probabilities calculated from averages over multiple trajectories



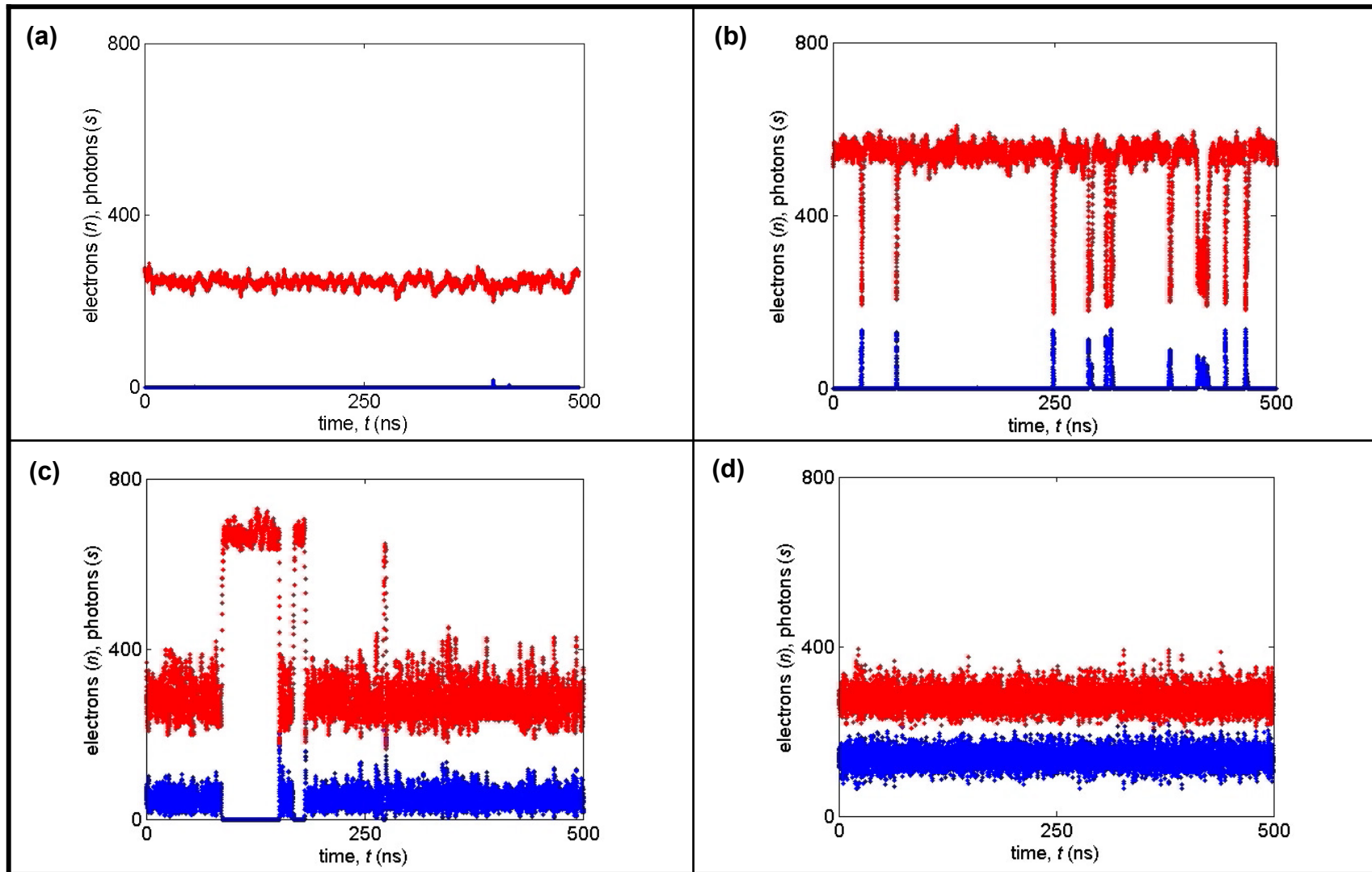
**Steady state master equation
solution to probability, $P_{n,s}$**



Monte Carlo solution to probability, $P_{n,s}$

Parameters : Volume = $0.1\mu\text{m} \times 0.1\mu\text{m} \times 10\text{nm}$, $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$, $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-4}$, $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$, $r = 1 - 10^{-6}$, $I = 192 \text{ nA}$.

System trajectories by Monte Carlo method



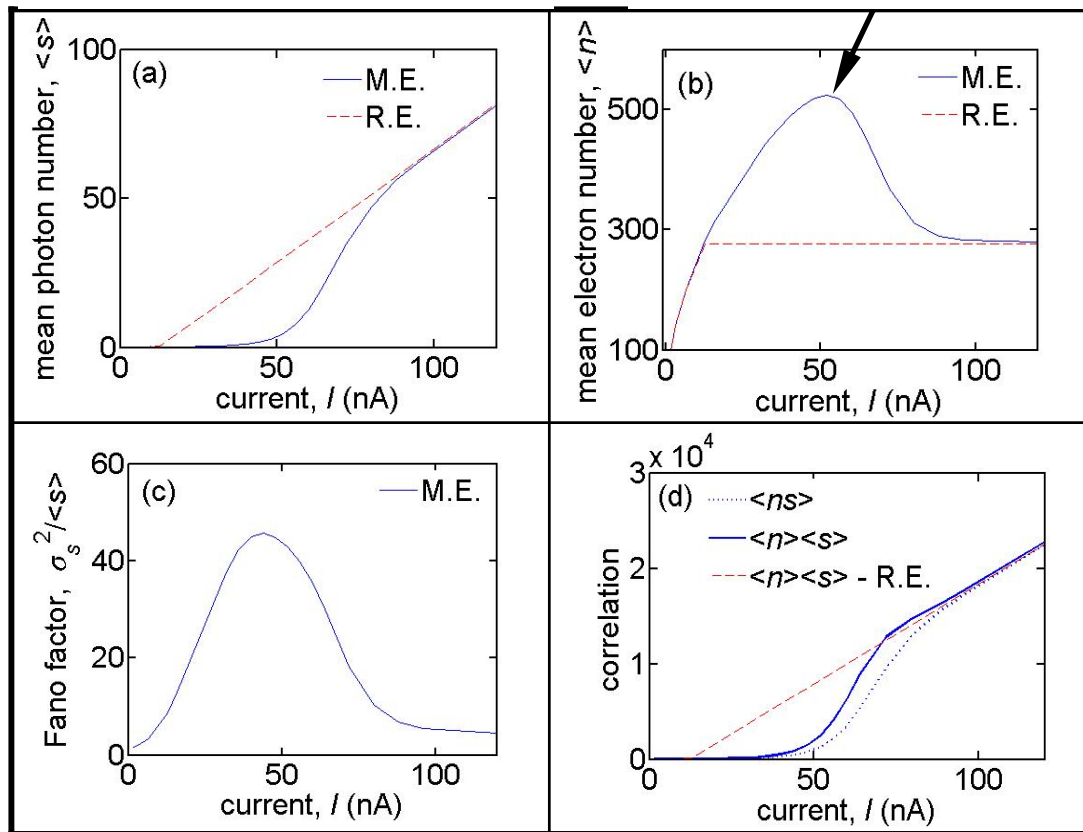
Parameters : Volume = $0.1\mu\text{m} \times 0.1\mu\text{m} \times 10\text{nm}$, $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$, $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-4}$, $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$, $r = 1 - 10^{-6}$.

Figure . (a) $I = 9.6 \text{ nA}$. (b) $I = 48 \text{ nA}$. (c) $I = 72 \text{ nA}$. (d) $I = 192 \text{ nA}$. **Electrons (red), photons (blue).**

Master equation predictions for small cavity

Suppression of
lasing
due to fluctuations

De-pinning of
carriers



$\langle ns \rangle$ does not factorize ($\langle n \rangle \langle s \rangle$) in the **small cavity** limit leading to **suppression** of lasing and **de-pinning** of carriers.

Parameters : Volume = $0.1 \mu\text{m} \times 0.1 \mu\text{m} \times 10 \text{nm}$, $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$, $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-4}$, $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$, $r = 1 - 10^{-6}$.

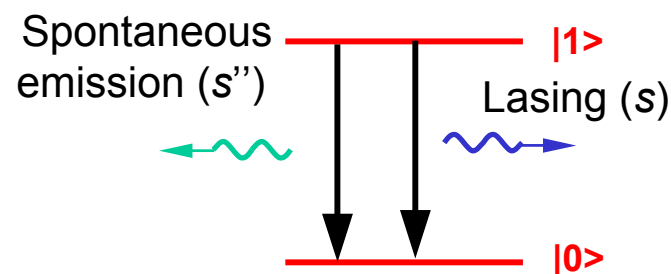
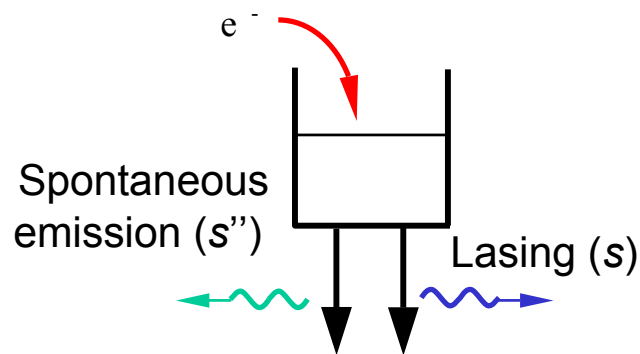
Figure . (a) $I = 9.6 \text{ nA}$. (b) $I = 48 \text{ nA}$. (c) $I = 72 \text{ nA}$. (d) $I = 192 \text{ nA}$.

Master equation involving **two** emission modes

- **Must account for each electron – so if it is not creating lasing photons – where is it going?**
- Excess electrons create photons of another emission mode (p) which decays at the same rate as lasing photons and does not participate in any stimulated processes.

$$\begin{aligned} \langle P_{n,s} \rangle' = & -\kappa(s P_{n,s,s''} - (s+1) P_{n,s+1,s''}) - (sG_n P_{n,s,s''} - (s-1)G_{n+1} P_{n+1,s-1,s''}) - (sAP_{n,s,s''} - (s+1)A P_{n-1,s+1,s''}) \\ & - \beta B(n^2 P_{n,s,s''} - (n+1)^2 P_{n+1,s-1,s''}) - (1-\beta)B(n^2 P_{n,s,s''} - (n+1)^2 P_{n+1,s,s''-1}) - I(P_{n,s} - P_{n-1,s}) \\ & - \kappa(s P_{n,s,s''} - (s+1) P_{n,s+1,s''+1}) \end{aligned}$$

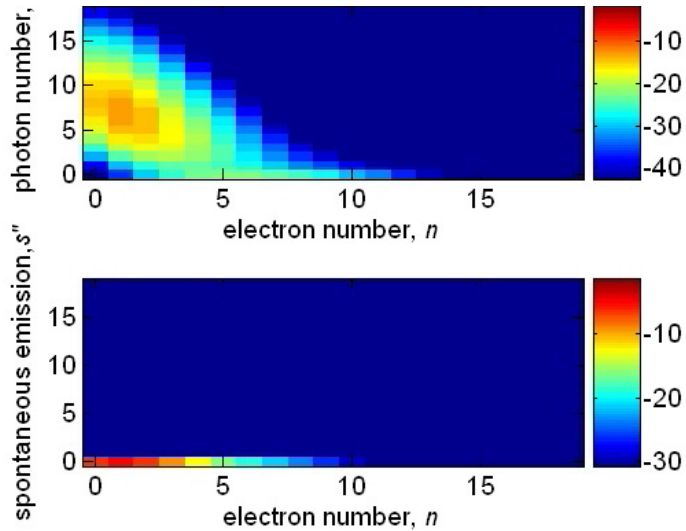
where $P_{n,s,s''}$ is the probability of a state having n electrons, s lasing photons, s'' non-lasing photons.



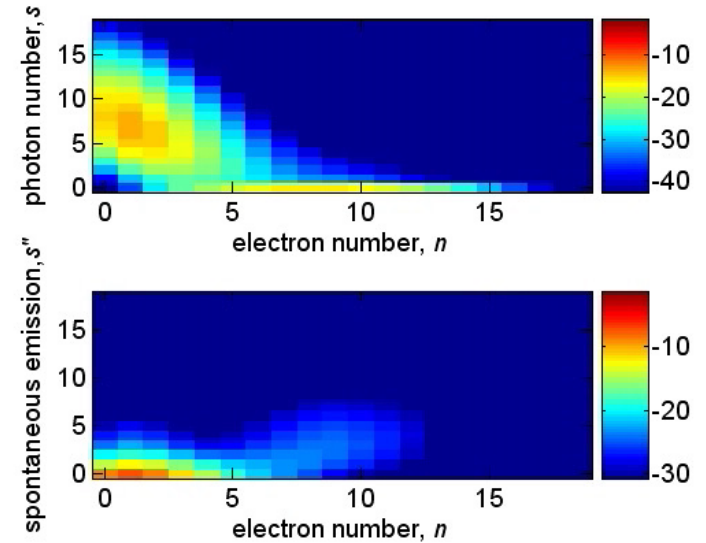
Probability distributions for different β

Parameters : $(1\mu\text{m} \times 1\text{nm} \times 1\text{nm}) = 1\text{e-}18 \text{ cm}^3$, $\Gamma = 0.25$, $a = 2.5\text{e-}018 \text{ cm}^2/\text{sec}$, $B = 1\text{e-}10 \text{ cm}^3/\text{sec}$, $n_g = 1\text{e+}18 / \text{cm}^3$, $\alpha_l = 10 \text{ cm}^{-1}$, $n_r = 4$, $r = 0.999$, $\kappa = \kappa_{\text{calc}} * 1\text{e-}2$, $P = 10 \text{ electron/ns}$ ($= 1.6 \text{ nA}$).

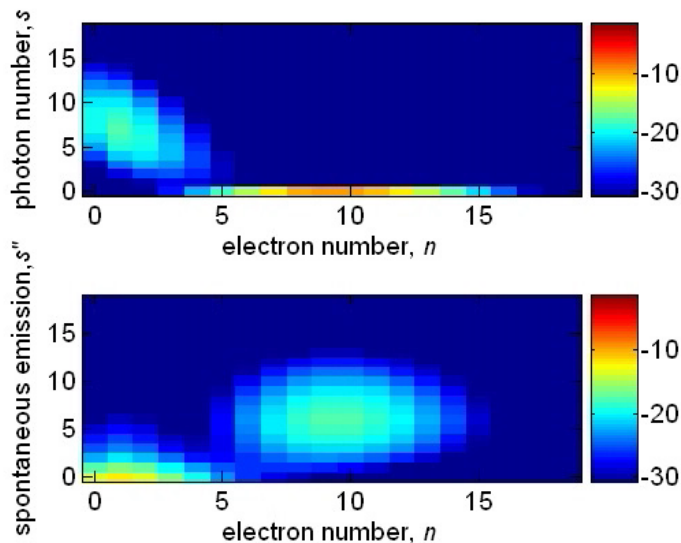
$\beta = 1$



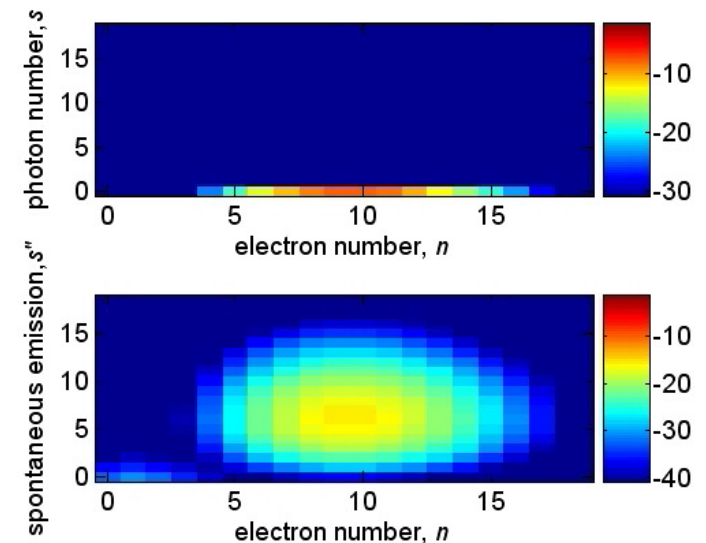
$\beta = 0.1$



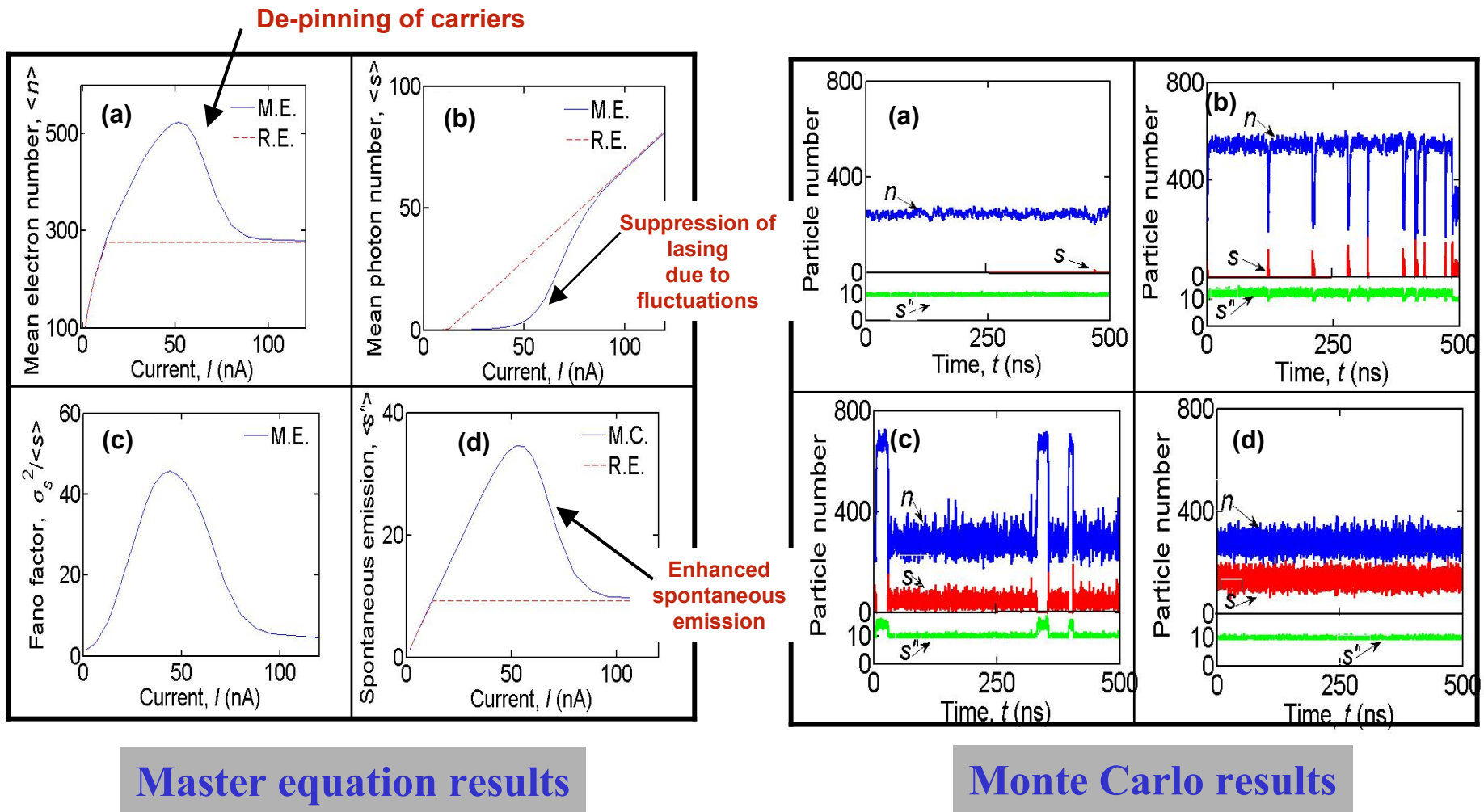
$\beta = 0.01$



$\beta = 0.0001$



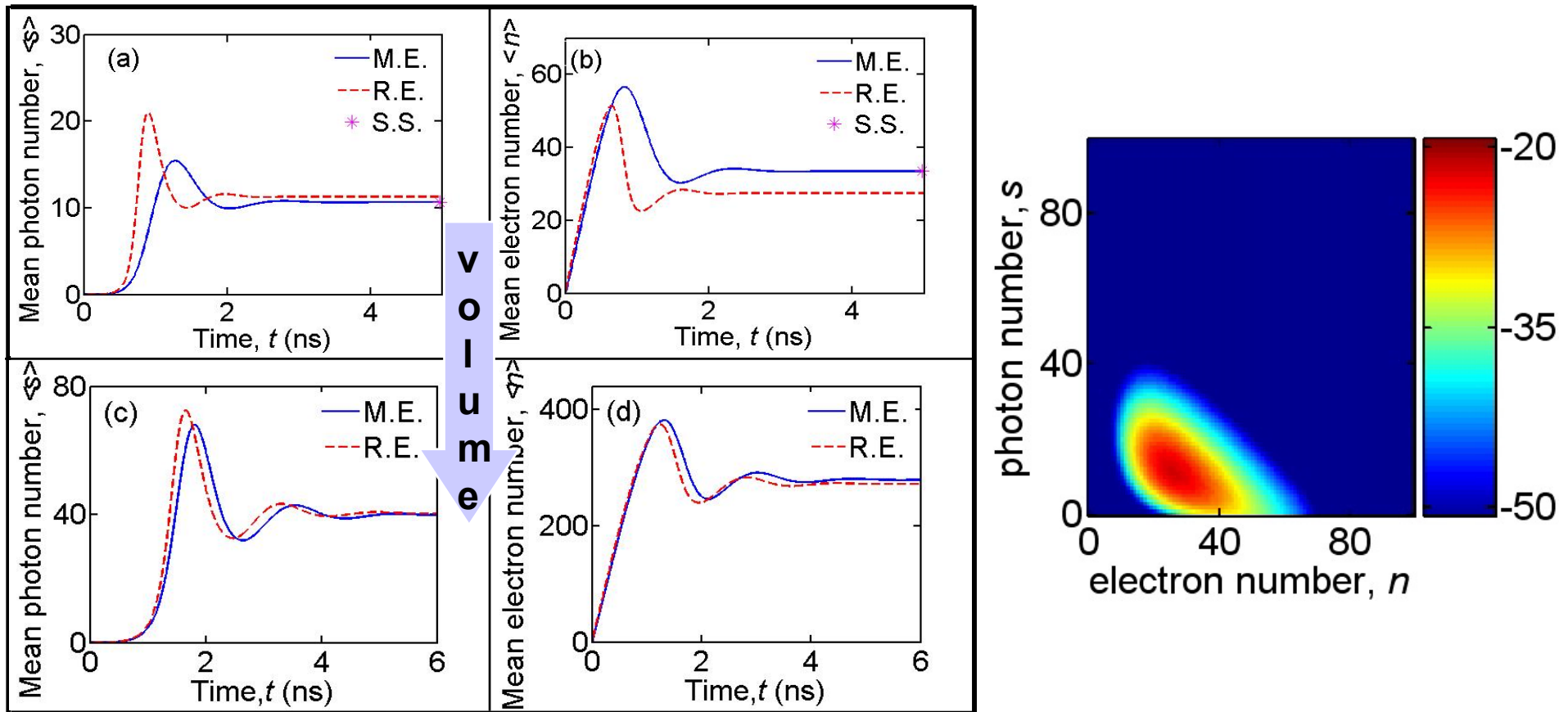
Comparison with random walk predictions



Parameters : Volume = $0.1\mu\text{m} \times 0.1\mu\text{m} \times 10\text{nm}$, $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$, $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-4}$, $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$, $r = 1 - 10^{-6}$.

Figure . (a) $I = 9.6 \text{ nA}$. (b) $I = 48 \text{ nA}$. (c) $I = 72 \text{ nA}$. (d) $I = 192 \text{ nA}$.

Temporal characteristics with system size

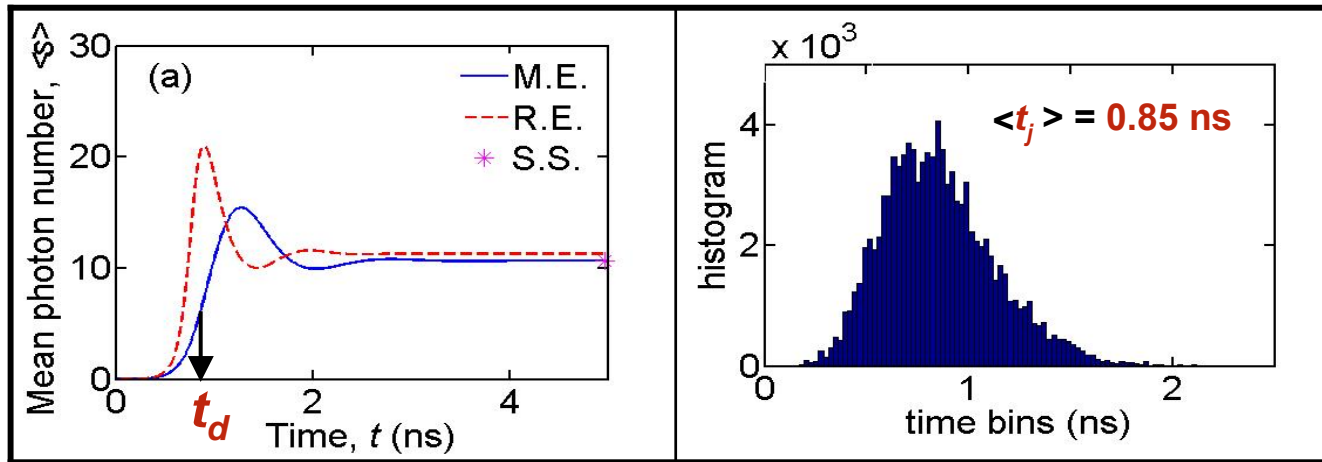


Parameters : $L_c = 0.1 \mu\text{m}$, $\Gamma = 0.25$, $a = 2.5e-018 \text{ cm}^2/\text{sec}$, $B = 1e-10 \text{ cm}^3/\text{sec}$, $\beta = 0.1$, $n_g = 1e+18 / \text{cm}^3$, $\alpha_l = 10 \text{ cm}^{-1}$, $n_r = 4$, $r = 0.999$, $\kappa = \kappa_{\text{calc}} * 1e-2$.

Figure . Transient behavior of first moments of electrons and photons for $P = 100 \text{ electron/ns}$ ($= 16 \text{ nA}$). Transient Master equation results (blue) and rate equation results (red). (a) mean photon number vs time. (b) mean electron number vs time. ($0.1 \mu\text{m} * 10 \text{ nm} * 10 \text{ nm} = 1e-17 \text{ cm}^3$). (c) mean electron number vs time. (d) mean photon number vs time. ($0.1 \mu\text{m} * 0.1 \mu\text{m} * 10 \text{ nm} = 1e-16 \text{ cm}^3$).

Temporal behavior – large signal analysis

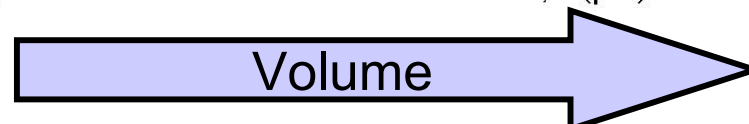
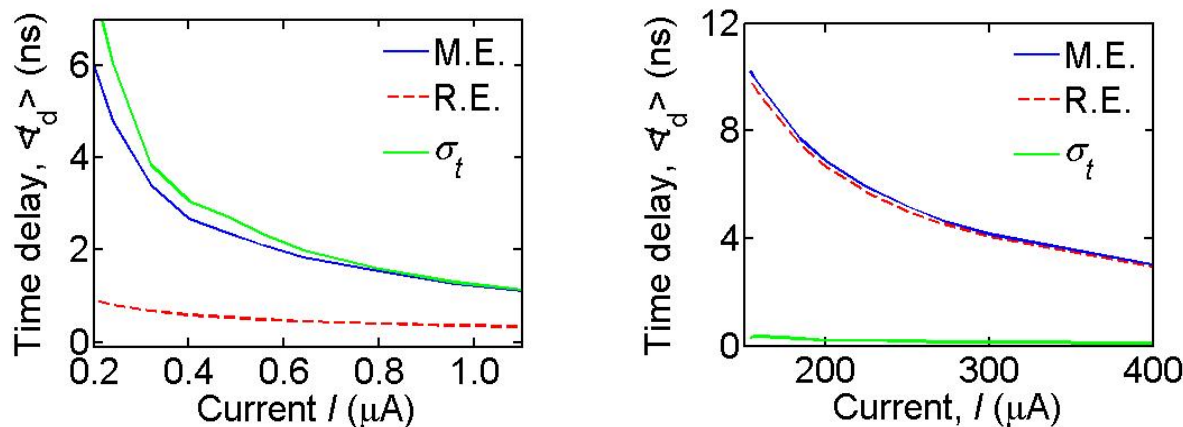
1. Response to a large step change in current (large signal)



Parameters :

Volume = $0.1\mu\text{m} \times 10\text{nm} \times 10\text{nm}$,
 $\Gamma = 0.25$, $a = 2.5 \times 10^{-18} \text{ cm}^2 \text{ s}^{-1}$,
 $B = 10^{-10} \text{ cm}^3 \text{ s}^{-1}$, $\beta = 10^{-1}$,
 $n_0 = 10^{18} \text{ cm}^{-3}$, $\alpha_i = 1 \text{ cm}^{-1}$, $n_r = 4$,
 $r = 1 - 10^{-6}$, $I = 16 \text{ nA}$.

2. Time jitter (t_d) decreases with increasing pump



Summary of steady-state calculations

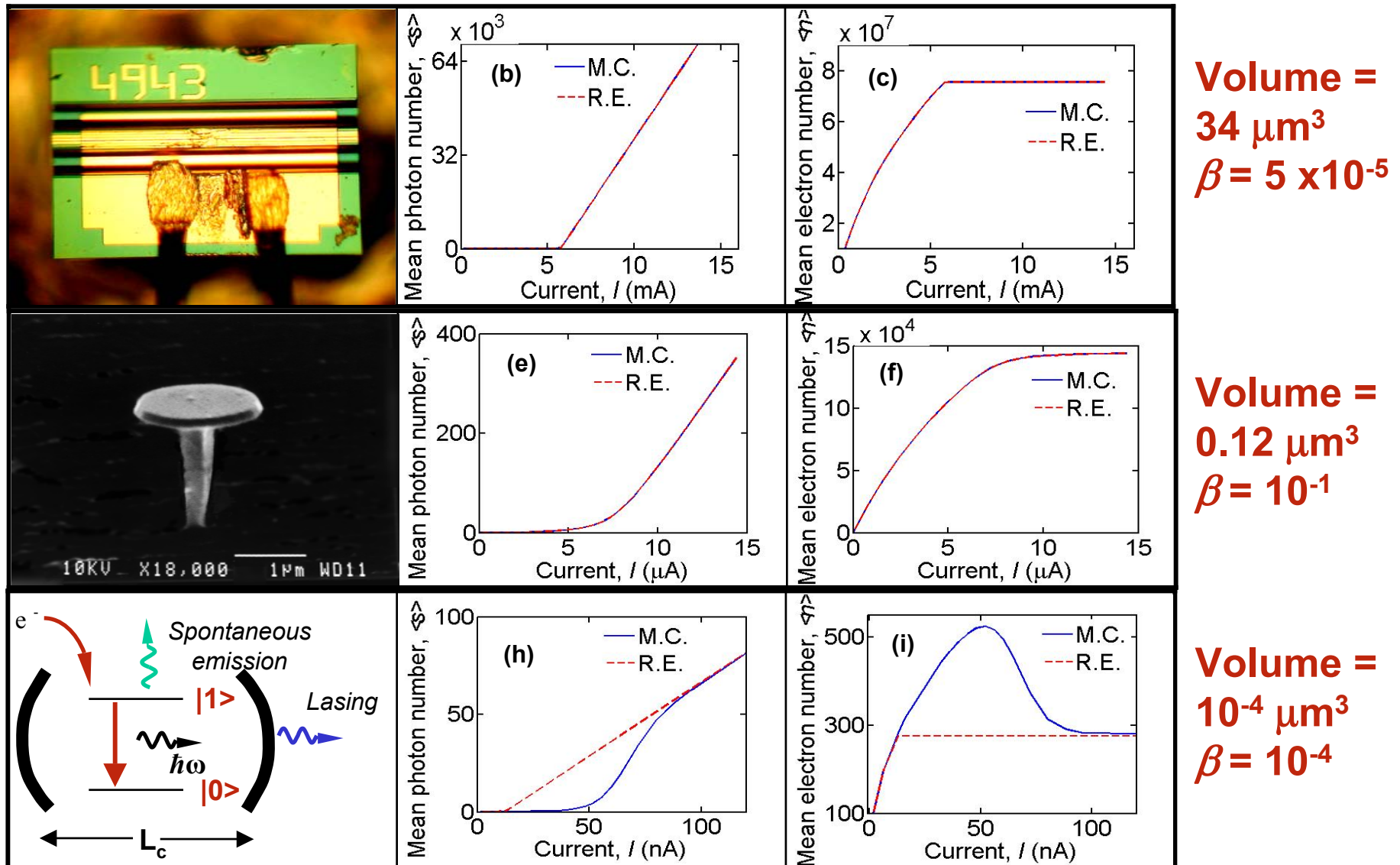
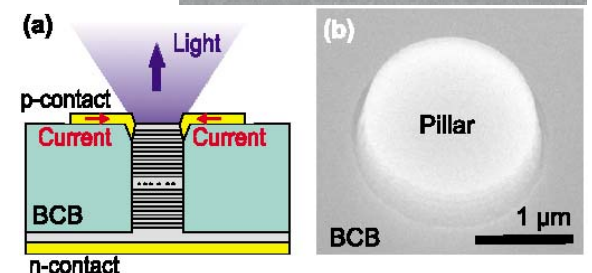
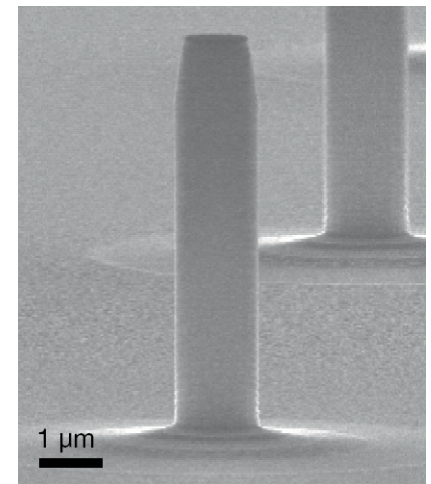
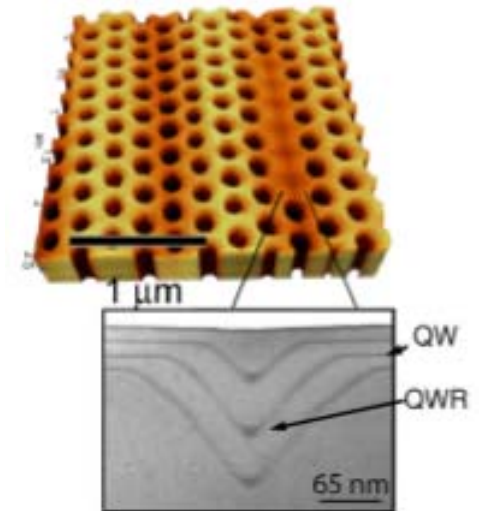


Figure . (a) Fabry – Perot laser. (d) Micro-disk laser. (g) Small laser (schematic diagram).
(b), (e), (h) Mean photon number vs current. (c), (f), (i) Mean electron number vs current.

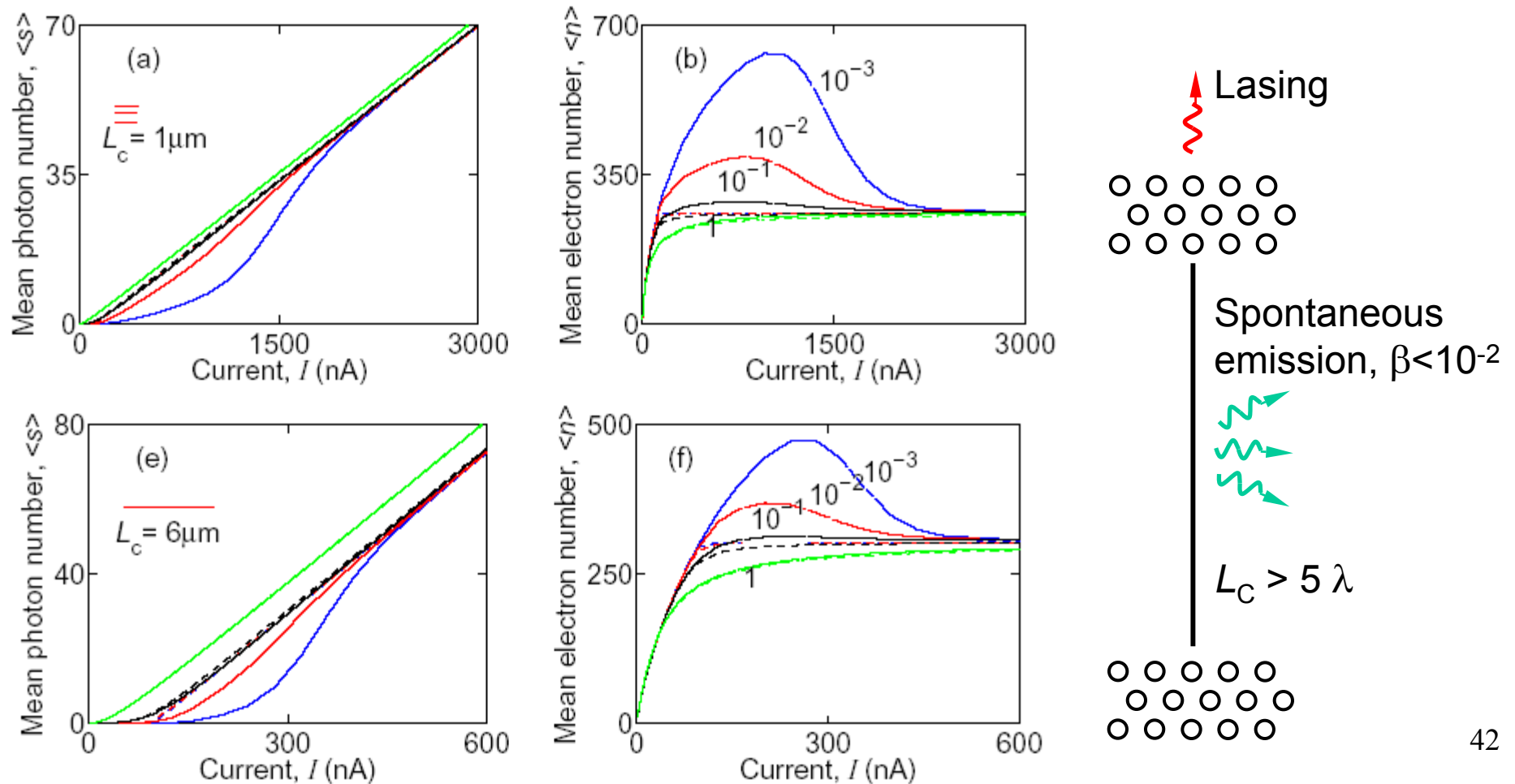
Making lasers with small active region volume

- **State-of-the-art quantum wire photonic crystal lasers and QD micropillar lasers can be made with very small active regions**
 - Active volume $V \sim 10^{-4} \mu\text{m}^3$ can have $n \sim 100 - 500$
- **Examples:**
 - **EPFL:** Kirill Atlasov, Eli Kapon, et al., “Short ($\sim 1\mu\text{m}$) Quantum-Wire Single-Mode Photonic-Crystal Microcavity Laser”, CTuH4 CLEO/IQEC 2009
 - Estimate active volume $V \sim 3 \times 5\text{nm} \times 5\text{nm} \times 1000\text{nm} = 75 \times 10^{-18} \text{cm}^3 = 0.75 \times 10^{-4} \mu\text{m}^3$
 - Fluctuations important since $n \sim 100 - 500$
 - **U. Würzburg:** A. Forchel et al., “Single quantum dot controlled gain modulation in high-Q micropillar lasers”, Phys. Status Solidi B **246**, No. 2, 277–282 (2009), Appl. Phys. Lett. **93**, 061104 (2008)
- **Quantum fluctuation effects should dominate device performance at low pump rates and $\beta < 10^{-2}$**



Making lasers with small active region volume

- Calculations suggest that observation of both enhanced spontaneous emission and suppression of lasing due to quantum fluctuations requires $\beta < 10^{-2}$



Conclusions

- 1. Fluctuations in n and s are important in determining the behavior of both large and small laser diodes**
- 2. In large lasers fluctuations in s play an important role in determining the temperature dependence of laser threshold current**
- 3. Quantum fluctuations in small lasers (and the fact that a ground state exists) can enhance spontaneous emission and suppress lasing near threshold (in contrast to predictions of Landau-Ginzburg in which fluctuations enhance emission below threshold). Dynamic switching between two characteristic system states dominates the fluctuations. Correlations between n discrete excited states and s discrete photons create a non-Poisson probability distribution and damp the average dynamic response of laser emission**

Finite sized systems behave differently and, in particular, fluctuations are important !

[Learn more: Phys. Rev. Lett. **102**, 053902 \(2009\)](#)

Acknowledgements

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